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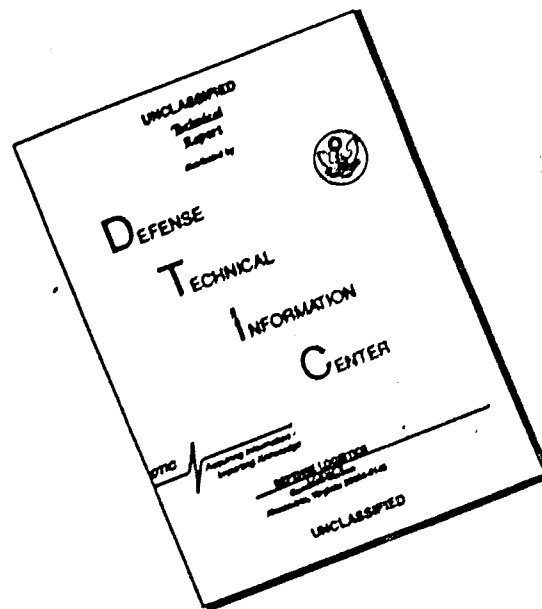


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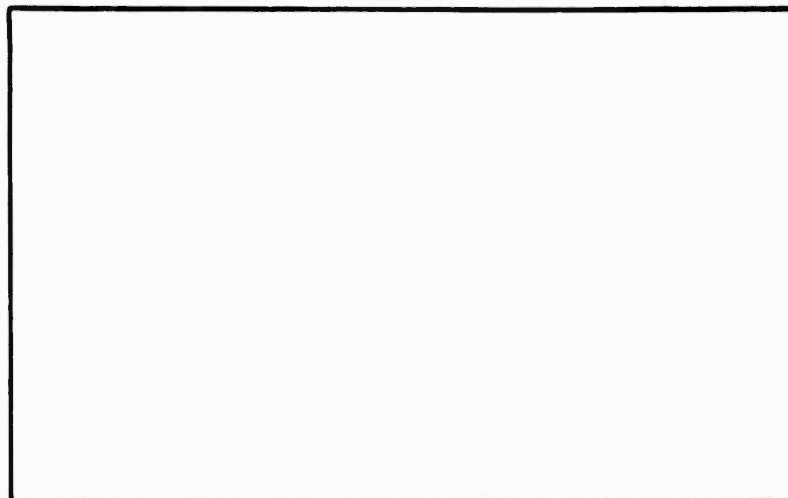
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A STUDY OF AN  
INDUCTION-COUPLED PLASMA  
OPERATING AT 400 KILOCYCLES

Howard R. Cannon

GA/Phys/62-2

A STUDY OF AN  
INDUCTION-COUPLED PLASMA  
OPERATING AT 400 KILOCYCLES

THEISIS

Presented to the Faculty of the School of Engineering of  
the Air Force Institute of Technology  
Air University  
in Partial Fulfillment of the  
Requirements for the Degree of  
Master of Science

By

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Preface

This report concerns an elementary investigation of the problems of containing an induction-coupled plasma, measuring the plasma power and temperature, and determining the effects changing plasma operating conditions. I hope this report successfully establishes a starting point for future detailed investigations.

During the period of this study I was the guest of the Aeronautical Research Laboratories, and I wish to thank the members of ARL, who made my visit informative and enjoyable. My thanks particularly to the staff of the Thermomechanics Laboratory, ARL, for their support and encouragement.

I am especially indebted to E. Isender for his guidance and support during his stay in this country, and to W. G. Braun and J. Birkeland, Plasma Physics Laboratory, ARL, for their explanation of Abel's Integral Transformation which appears in Appendix A. My thanks also to my lab partner, A. Shade, for the time and effort he devoted to assisting me, sometimes at the expense of his own study.

This report could not have been submitted in its present form without the patience and understanding of my Faculty Advisor, R. Wingerson. If time had permitted me to properly act upon his counsel, a far better report would have resulted.

And finally, my thanks to my wife, Carolyn, for her efforts to minimize distractions while I worked.

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List of Symbols

- $D_c$  - Diameter of Radio Frequency Induction Coil
- $D_p$  - Diameter of the Plasma
- $\eta$  - Power Coupling Effectiveness
- $\eta_c$  - Calorimeter Power Coupling Effectiveness
- $\eta_r$  - Radiation Power Coupling Effectiveness
- $\eta_L$  - Wall Loss Power Coupling Effectiveness
- $\eta_t$  - Total Plasma Power Coupling Effectiveness
- $i_c$  - Plate Power-Excess
- $i_r$  - Plate Power-Irradiation
- $i_t$  - Plate Power-Total
- $i$  - Power ratio
- $k_c$  - Calorimeter Power Ratio
- $k_r$  - Radiation Power Ratio
- $k_L$  - Wall Loss Power Ratio

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Abstract

A rf, electrodeless plasma-generator was developed which operated at peak plasma powers of 50 kw. The plasma was vortex stabilized, and was contained within a water-cooled Vycor tube. Power was measured calorimetrically. Radiation power was measured by alternately using clear water and water made opaque with India ink to cool the Vycor tube. A model temperature profile was deduced from spectrographic measurements transverse to the plasma axis. Maximum plasma temperatures were shown to exist in a thin cylindrical sheath near the plasma surface, with relatively cooler temperatures existing at the center-line gas back-flow. Effects of changing gas flowrate, gas composition, rf power, and Vycor tube diameter on the effectiveness of the energy coupling mechanism are shown.

A STUDY OF AN  
INDUCTION-COUPLED PLASMA  
OPERATING AT 400 KILOCYCLES

1. Introduction

An induction-coupled plasma is realized in a partially ionized gas by electrical currents which are inductively coupled to a radio frequency (rf) magnetic field. This method of plasma production is capable of generating plasmas free of the contamination which is characteristic of direct-current and alternating-current arcs. These arcs are contaminated by electrode erosion caused by the direct contact between the electrodes and the arc.

Induction-coupled plasmas are "electrodeless arcs" and there is no direct contact between the plasma and the rf power supply.

Origin of the Study

H. Pfender of the Institut fuer HeiBstrahlungsforschung, Stuttgart-Deerloch, Western Germany, initiated this study while he was engaged in research work at the General Electric Research Laboratories (R&D), Wright-Patterson AFB, OH, at the direction of H. Joehngen, Chief of the Thermomechanics Laboratory, R&D. H. Pfender is interested in this plasma because it provides a possible source of electrons, ions, and neutral atoms which are in local thermal equilibrium (Ref. 2: 824), while H. Joehngen was primarily interested in the energy transfer characteristics exhibited by this plasma coupling mechanism.

### Statement of Problem

The objectives of this study were (1) to operate a stable plasma at atmospheric pressure at 400 kilocycles (kc) with a sustained, high-power operation capability, (2) to determine the temperature profile of the plasma as a function of the plasma radius,  $T(r)$ , (3) to measure the power transmitted to the plasma, and (4) to determine parameters important to the energy coupling mechanism.

### Experimental approach

The plasma was contained in a water-cooled Vycor tube (Fig. 1), and was stabilized in the vortex flow resulting from tangential gas injection in the manner prescribed by T. B. Reed (Ref. 2: 822).

The temperature profile,  $T(r)$ , was deduced from intensity profiles,  $I(x)$ , of the lambda 7635ÅI and lambda 4861ÅII spectral lines obtained by spectrographic scans transverse to the plasma axis.

The total power transferred to the plasma was determined by measuring the power the plasma transferred to cooling water. Radiation power was measured by circulating an opaque coolant instead of clear water about the Vycor tube which contained the plasma (Fig. 2).

The parameters varied in this study were rf power delivered by the power supply, gas flow, the diameter of the Vycor tube containing the plasma, and the gas composition. The rf power was varied by changing the plate voltage of the power supply, and the gas composition was changed by mixing helium and argon.

Possible Uses

As stated by Reed, (Ref. 2: P24),

"It is still too early to say what the capabilities and limitations of inductive plasma generation are. We have used the plasma torch to grow single crystals of refractory oxides, and oxygen-containing plasmas will melt aluminum oxide ( $m.p. = 2700^{\circ}K$ ). The temperatures achieved in the plasma will depend ultimately on the power available and the nondestructive containment of the plasma. Presumably, the induction plasma will find use wherever the dc plasmas are used, from measurement of spectral transition probabilities to preheating gases for use in hypersonic wind tunnels."

In addition to preheating the gases for use in hypersonic wind tunnels, stagnation temperatures attainable in hypersonic wind tunnels can be increased by heat addition in the supersonic flow section using an induction-coupled plasma.



## II. Experiment

### Description of Apparatus

Part of the experimental apparatus is shown in Figure 3. In the background is the rf power supply. Starting at the extreme left, the apparatus seen is a portion of the gas supply bottle, the vacuum pump and vent, the vacuum pump shut-off valve, the exhaust valve, and the vacuum system pressure gauges. The pressure gauges are mounted on the support stand. Above the support stand the calorimeter jacket, plasma-generator, and the support stand scaffold are seen. Behind the calorimeter jacket two meters are seen, which were not pertinent to this study. The drape covers other equipment which was not pertinent.

Gas Supply System. The argon and helium used in this study were supplied by the Burdett Oxygen Company, and contained no more than one percent impurities by volume. Gas flows were measured by Airco Dual Range Flowmeters for Argon, style number 805-1601. These meters were calibrated from 1 to 106 standard cubic feet per hour (scfh). Gas flows in excess of 106 scfh were measured by using the meters in parallel. Helium flowrates were obtained from the argon flowmeter readings by use of conversion graphs furnished by Airco.

Plasma-Generator. The water-cooled plasma-generator was made in four pieces, the top and bottom end-pieces, and the inner and outer tubes (Fig. 4). The end-pieces were made of brass, the outer tube was Pyrex, and the inner tube was Vycor. Standard rubber O-rings coated with high vacuum silicone grease provided the seals between the end-pieces

and tubes.

The top end-piece contains the gas inlet, the gas injection plate, and the coolant outlet. In the gas injection plate are eight 0.45-in.-diameter holes equally spaced on a two-inch-diameter circle. The holes are 0.001-in. deep and extend to the face of the injection plate. As the gas enters the inner tube through these holes, the plasma-stabilizing vortex is formed. The coolant outlet is a piece of 3/8-in. copper tubing.

The bottom end-piece contains the hot-gas exhaust port, the coolant inlet, and the coolant manifold. The hot-gas exhaust axially through a 72-mm-diameter port, and a piece of 3/8-in. copper tubing provides the coolant inlet. The coolant enters and leaves the coolant manifold axially to prevent stagnation areas from forming in the coolant as it circulates between the inner and outer tubes. The coolant manifold was formed by machining a groove in the bottom end-piece. The coolant leaves the coolant manifold through the annulus formed by the inner tube and the 72-mm-diameter hole that forms the top of the manifold. This narrow exit annulus (1.4-in. wide) shields the coolant between the tubes from the gas inlet effect at the coolant inlet. This permits an upward spirally flow pattern, free of stagnation areas, to exist between the tubes.

The tubes are mounted co-axially between the end-pieces. The inner tube is a Vycor tube 18-in. long with a nominal 75-mm outside diameter. Vycor was required because the inner tube must be capable of supporting a severe temperature gradient. On many occasions it was

observed that while the outer surface of the Pyrex tube remained at water temperatures, the inner surface was glowing red hot. The outside diameter is listed as a nominal 75-mm because variations in this diameter of plus or minus one or two millimeters are common, and the tubes are often out-of-round. Because of these irregularities, the ends of the Pyrex tubes must generally not be sized before they were used.

The outer tube was a Pyrex tube 1/2-in. long with a nominal outside diameter of 75-mm. The outer tube carries the axial compressive loads which are applied to hold the plasma-render tor together. The end-pieces are constructed in such a way that no axial or relative loads can be applied to the inner tube. This was done to prevent possible breakage of the inner tube by the combined effects of axial compression, thermal stresses, and hoop stresses caused by the pressure of the coolant.

Standard rubber O-rings were used to provide a seal between the end-pieces and the inner and outer tubes. Two O-rings were used at each seal to improve the reliability of the seal. Rubber gaskets were used to prevent direct contact between the ends of the tubes and the end-pieces to prevent chipping. The bottom end-piece is supported by the calorimeter and an O-ring provides the seal between these two parts.

Calorimeter. The calorimeter consists of a water-cooled jacket and two interior coils of copper tubing (Fig. 4). The water enters the outer shell of the jacket, flows in the outer shell, down the inner shell and then leaves the jacket. The cooling water next flows through the ascending coil of copper tubing, which is wrapped around the descending coil of copper tubing, and then through the descending coil and

out of the calorimeter. The coils of copper tubing were modifications made to existing equipment, and represent the simplest change that could be made. An existing joint in the exhaust pipe was separated and the cooling coils were inserted into the exhaust pipe. The cooling arrangement that resulted was not ideal, but it was adequate. The temperature of the exhaust gas was measured after the gas left the calorimeter, and the heat power remaining in the exhaust gases at this point was approximately 0.3 Btu per lb. After the gas leaves the calorimeter, it can be directed to the atmosphere or to a vacuum pump.

Vacuum system. The vacuum system used was constructed by Henry W. Dutton, patent number 16,9315. This is a single-stage, rotary-vane, oil-sealed pump. The pump was capable of reducing the pressure in the plasma generator to .1-mm of mercury, absolute (mm Hg abs), under no-flow conditions.

Vacuum pressures were read on a vacuum pressure gauge calibrated from 2-mm Hg abs to .1-mm Hg abs. A pressure of interest was below 1.0-mm Hg abs for 15 seconds before the plasma was attained, it indicated satisfactory seals in the plasma-generator, and a start could be made. The plasma was not operated in a vacuum other than during starting. A second pressure gauge in the system, which read pressures above and below atmospheric, in inches of mercury, was used to determine the appropriate time for opening the exhaust valve. The exhaust valve was opened when the pressure gauge indicated atmospheric pressure.

Coolant system. The coolant system consisted of a coolant supply, the plasma-generator, the calorimeter, flowmeters, and connecting lines.

The primary coolant was tap water, but an alternate coolant supply was available for use in the plasma-generator. The alternate coolant was "black water" and was used to measure radiation power. The black water was a mixture of Carter's India ink, tap water, and aqueous ammonia. The approximate proportions used were 30 gallons of water, three pints of India ink, and one pint of ammonia. The ink was added to the water until the plasma was no longer visible through the plasma-generator, and the ammonia was added to prevent the ink from separating out of the water.

During operation, the black water was recirculated through a pulverized drum. The water which flowed through submerged cooling coils in the drum removed heat from the black water as it recirculated. The recirculating pump could deliver 1500 pounds of water per hour at 34 psi, whereas the tap water supply provided 1000 pounds per hour less water and six psi less pressure than the tap water supply provided. The higher flowrate for tap water was used to inhibit nucleate boiling in the plasma-generator, because nucleate boiling leaves mineral deposits on the inner tube which interfere with radiation measurements.

Selector valves in the plasma-generator coolant lines permitted a shift to black water without the necessity of stopping the plasma. A bypass line was put in the black water system to permit operation of the recirculating pump at any time.

Coolant inlet pressure was monitored during the runs. In general, the black water pressure remained constant, but occasional high frequency fluctuations were noted. The tap water pressure was often varying up and down as much as two psi several times a minute.

Coolant flow to the plasma-generator was measured by four Fisher and Porter Stabl-Flow Rotameters in parallel, and water flow to the calorimeter was measured by a Fisher and Porter Flowmeter. The Rotameters and Flowmeter are accurate to the nearest five pounds per hour. The rotameters could not be read when operating with black water, however, sufficient time was available between the time black water was selected and the time it reached the rotameters to allow the new flow indication to stabilize and be read. Hereafter, the black water flow was considered constant, which appears to be a good assumption based upon the constant black water inlet pressure.

Temperature Recording System. The temperature recording system consisted of three Channel Thermocouples, a cold junction, and a continuous recording galvanometer. The recording galvanometer used was a Honeywell Visicorder, Model 9565-159000. The system was calibrated at ice bath temperature, boiling water temperature, and at 90°F and 150°F. The meter was linear over this temperature range, with an average sensitivity of 95°F per inch. The Visicorder traced a ten-lines-per-inch scale on the trace, and the temperature traces were about 1/20-in. wide. The deflection of the center of the temperature trace was read to the nearest 1/40-in. Recordings were simultaneously made of the coolant inlet and outlet temperatures, and of the exhaust

and temperature after the gas left the calorimeter.

Support Stand and Scaffold. The calorimeter was mounted in the support stand (Fig. 3). The calorimeter supported the bottom of the plasma-generator, and the support stand scaffold restrained the top of the plasma-generator. The restraining force applied to the top of the plasma-generator was necessary to hold the plasma-generator together because of the pressure of the coolant in the plasma-generator. The force on the top end-piece caused by this pressure was strong enough to cause the original wooden cross-bar of the scaffold to bend and thus allow the top end-piece to move. For this reason, an aluminum channel was used to reinforce the cross-bar, and then the restraining force was adjusted so that the top end-piece did not visibly move when the coolant was turned on. The outer tube of the plasma-generator is required to carry this load, and also the load resulting from the vacuum in the inner tube, before the coolant is turned on.

Rf Power Supply. The rf power supply was a Westinghouse power oscillator rated at 200 kw at 400 kc. The power output of this oscillator could be controlled by selection of one of the nine discrete plate voltages available, and then selection of duty cycle. The plate voltage could not be changed while the power supply was operating, however, the duty cycle could be varied at any time from 0-100%. At duty cycles less than 100%, the rf power was delivered in pulses of varying lengths depending upon the duty cycle selected. The pulse rate was 360 per second. A duty cycle of 50%, then, resulted in pulse lengths of 1/720 second. A 100% duty cycle was used for this study, except during starting.

### Experimental Procedures

The experimental procedures will be grouped into three categories. These three categories are (1) pre-starting procedures, (2) starting procedures, and (3) data run procedures. The tasks covered under each category will be presented in a logical order of sequence, and will be so arranged that only those items which need special attention will be included in the description of typical operation of the engine.

Pre-starting Checks. The checks to be made prior to starting the engine should be accomplished in the following order to insure safe operation of the engine, and to prevent damage to the engine. The first check is to make sure the engine is properly lubricated. The oil level should be checked, and if necessary, the oil should be added. The oil should be added to the oil sump, and the oil level should be checked again. The second check is to make sure the engine is properly cooled. The coolant level should be checked, and if necessary, the coolant should be added. The coolant should be added to the coolant reservoir, and the coolant level should be checked again. The third check is to make sure the engine is properly charged. The battery voltage should be checked, and if necessary, the battery should be charged. The battery should be charged using a battery charger, and the battery voltage should be checked again. The fourth check is to make sure the engine is properly adjusted. The throttle linkage should be checked, and if necessary, the throttle linkage should be adjusted. The throttle linkage should be adjusted so that the throttle is fully open when the accelerator pedal is fully depressed. The fifth check is to make sure the engine is properly grounded. The ground connection should be checked, and if necessary, the ground connection should be made. The ground connection should be made to the engine block, and the ground connection should be checked again. The sixth check is to make sure the engine is properly secured. The engine should be secured to the frame, and the engine should be checked again. The seventh check is to make sure the engine is properly protected. The engine should be protected from the elements, and the engine should be checked again. The eighth check is to make sure the engine is properly maintained. The engine should be maintained in good condition, and the engine should be checked again. The ninth check is to make sure the engine is properly stored. The engine should be stored in a dry, clean, and well-ventilated area, and the engine should be checked again. The tenth check is to make sure the engine is properly disposed of. The engine should be disposed of in a safe and proper manner, and the engine should be checked again.

If the vibration is satisfactory, the coolant system is turned on, and a check is made for leaks. Gradually, water will seep into the inner tube even though the vacuum checked below 1.0 mm Hg abs.



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When this occurs, a leak in the vacuum usually appears and ice will form where the water enters the inner tube. Small leaks of this nature can often be stopped by taping the end-leaves and thereby reducing the leakage. If this effort fails, it is necessary to disassemble the plasma-generator and change the end-leaves of different sizes.

If no leaks are apparent, the contact inlet pressure is raised to 40 psi, and the flow meters are checked for normal readings. The flow to the plasma-generator should be approximately 200 gms per hour, and the flow to the multiplier should be about 100 gms per hour. The multiplier should be adjusted in order to obtain the time required for production of the required amount.

Normal flow of gas is indicated by the black water system, but the flow of this water can be checked by observing the sound of the re-irradiation pump, by observing the circulation in the main tank, and by the flow of gas in the main tank through the by-pass line.

After the contact again exhibits proper operation, the vacuum is slowly released and the top end-leaves are observed for possible movement. Any movement of the top end-leaves is corrected by increasing the contact pressure.

With the completion of these tests, a final check of the plasma operation are assured. However, the plasma generator should be checked for an hourly supply of recording tape, and the multiplier should be checked for a supply pressure of approximately 100 psi to insure sufficient tape and gas for a later run.

Starting Procedure. The starting procedure is not included in the data run section because special attention should be given to this critical portion of the plasma operation. The plasma is started in an argon atmosphere at an absolute pressure less than  $1.5 \times 10^{-4}$  torr. It requires about  $1.5 \times 10^{-4}$  torr to start the plasma. The starting may be obtained at lower rf power settings, also, but the possibility of over tube discoloration is increased. The discoloration is permanent when the plasma is started the first time, as it does when operated at the pressure, if the rf power is too high.

When the starting pressure has been reached, the rf power supply is turned on, and the duty cycle is gradually increased until a pale pink glow is seen in the plasma-generator. At this time, the valve to the vacuum pump is turned off, because the pump is no longer needed and because this method leads to a more rapid pressure build up in the plasma. The vacuum pump valve is now turned on, and the pale pink glow turns into a brilliant blue-white flame. The next five to ten seconds is the most critical period of plasma operation. The flow is gradually increased to about 75 cc/hr, while the power is gradually increased to maintain the pressure rise associated with the gas flow. Should the power be increased too slowly, the plasma will extinguish; if the power is increased too rapidly, the plasma will contact the tube with sufficient energy to fire for it. This discoloration is permanent and precludes the use of the tube in radiation measurements.

The danger of discoloration rapidly decreases (due to plasma contraction) as the pressure and gas flow increase. As soon as the plasma contraction is noticed, the rf power may be increased fairly rapidly to a duty cycle setting of approximately 50%. Meanwhile, a close check on the plasma pressure is maintained, and as the pressure again reaches zero, the exhaust valve is opened. When this task has been accomplished, the starting procedure is complete.

Data Run. The data run begins when the gas flow is increased to the maximum value of 25 scfh, attainable, and the duty cycle is adjusted to 100%. The duty cycle remains on 100% for the remainder of the data run, while the gas flow is reduced in 25 scfh increments, until a flow of 100 scfh is reached. As soon as temperature equilibrium for each flow rate is indicated by the traces on the Visicorder tape, the tape is moved with the gas flow, and all meters are read. The meters read are the rf power supply plate voltmeter and plate ammeter, and all the water flowmeters.

A lower limit of 100 scfh on the gas flow was established because at flows less than 100 scfh, coolant boiling becomes substantial enough to cause mineral deposits to form on the inner tube, which interfere with radiation measurements.

After readings for a gas flow of 100 scfh are taken, the gas flow is increased to its maximum value as before, and the plasma-generator coolant supply is switched to black water. The coolant flowmeters must be read as soon as the coolant flow indications stabilize. There is

sufficient clear water in the coolant system ahead of the black water to allow the stabilized flow-indications to be read, before the flow indicators are obscured by the black water. The black water flowrate is assumed constant for the remainder of the data run. This assumption is reasonable since the black water supply pressure remains constant except for occasional indications of high frequency fluctuations of plus and minus 1/2 psi. The origin of these fluctuations is unknown, however, the fluctuations did not appear to effect coolant flowrate.

With the exception of the assumed constant values of black water flow, meter readings are obtained at 25 scfh flow increments as before. After the final set of readings are taken, the gas flow is increased to maximum value, and the duty cycle percentage is decreased, prior to turning off the rf power supply. This was done to cool the inner surface of the inner tube gradually enough to prevent post-operating tube cracks, which result from residual stresses caused by rapid cooling.

After the rf power supply was turned off, the clear water coolant supply was again selected, thereby flushing the black water from the coolant lines.

#### Physical Appearance of Plasma

The plasma first appears as a brilliant blue white discharge, in the vicinity of the rf induction coil, the instant the argon gas flow commences during the starting procedure. The plasma appears to extend out to the Vycor tube when operating at this low pressure. As the pressure and gas flow increase, the plasma contracts so that the

luminous gases no longer appear to contact the tube wall. The plasma is now shaped as a cylinder five to six inches in length and roughly centered in the rf coil area. This general shape is maintained until the gas flow approaches 60 scfh. At this gas flow, the top edge of the plasma intermittently extends up to the injection plate in the top end-piece. As the gas flow is increased to 70 scfh, the back-flow of gases up the center of the tube becomes strong enough to cause the top edge of the plasma to become permanently extended. The diameter of the extended portion of the plasma is largest level with the top of the rf coil, and is smallest at a point about two inches below the injection plate (Fig. 4). At this point the plasma begins to diverge toward the inlet holes in the injection plate. During the increases in gas flow, the bottom edge of the plasma extends downward slightly. Below the bottom coil, the brilliance of the plasma fades very sharply into a ragged-edged tail-flame approximately one inch long.

This description is representative of typical plasma operation. The dimensions of the plasma were not measured, and all stated values are approximations. Further, the dimensions of the plasma, and the gas flows at which plasma extension occurs are strongly dependent upon the rf power level. More important than the exact dimensions of the plasma are the changes in appearance of the plasma which result from changes in rf power and gas flow. Within the range of rf power and gas flow used in this study, increasing the rf power increases the diameter of the plasma and increases the length of the tail-flame, while increasing the gas flow decreases the diameter of the plasma, and increases

the length of the tail-flame. The changes due to changing rf power were observed by changing the duty cycle. After the rf power and gas flow were set for a data run any changes in the brilliance of the plasma were too subtle to be detected by eye. Due to the intense brightness of the plasma, it was normally observed for a dark green plasma.

### Temperature Profile

A method for analyzing the temperature profile of an arc plasma is explained by H. L. Loch, *Rev. Sci. Instr.*, 1: 191. In brief, this method is based upon the temperature dependence of the normalized relative intensities of the atomic hydrogen  $H\alpha$  and  $H\beta$  lines and the Lyman  $\alpha$  and  $\beta$  lines. The observed intensities of these lines along a distance,  $I(x)$ , are converted into intensities which are functions of the radius,  $I(r)$ , by the following integral (Appendix A). The line intensities are differentiated with respect to  $x$ .

$$J(r) = -\frac{1}{\pi} \int_r^R \frac{N'(x) dx}{\sqrt{x^2 - r^2}} \quad (1)$$

Figure 6 shows the results obtained by converting observed  $I(x)$ 's to radial distributions,  $I(r)$ 's using this integral, and then normalizing each curve with respect to its maximum intensity. This figure clearly shows that  $I(r)$  has a more pronounced dip at  $r$  equal zero, than does  $I(x)$  at  $x$  equal zero. The temperature profile,  $T(r)$ , may now be plotted by taking the normalized relative intensity of one of the

spectral lines from Figure 6 for a particular radius, and obtaining the corresponding temperature from Figure 5. At this point, it is well to note that an ambiguity exists when using a single spectral line to determine temperature. With a normalized relative intensity of 0.85, it is possible to obtain values for temperature of either 14,000K or 16,500K. This ambiguity is solved by the presence of a measurable intensity of lambda 4964Å, which indicates temperatures above 15,000K; or by the absence of this line, which indicates temperatures less than 15,000K.

The investigation of the temperature profile of the plasma under study here is not complete. However, sufficient preliminary investigations were made to justify certain conclusions concerning the temperature distribution.

The intensity of lambda 4964Å,  $I(x)$ , was recorded for various using successively higher power levels. The recorded  $I(x)$ 's showed maximum values off the center-line (Fig. 2). The recorded maximum intensity and the center line intensities increased as a result of the first power increases. The power level was raised with successive increases in power and the off-center intensities began to increase, and the center-line intensities began to stabilize. These off-center peak intensities were now interpreted to be the location of the 15,000K isotherm. Since the center-line intensities as  $I(x)$ , were always less than the off-center maximums, even when these off-center

maximum could not be identified with the 15,000°K isotherm, it was concluded that the center temperature was less than 15,000°K. If, however, these low center-line intensities were indicative of temperatures above 15,000°K, the temperature would have to be in excess of 20,000°K. At this temperature, the Lyman  $\alpha$  line should show a strong intensity in the center-line, provided the temperature did not exceed 20,000°K. The presence of the Lyman  $\alpha$  line was detected in the plasma, but only very faintly, and in a constant intensity across the plasma. This finding was interpreted as proving the existence of a temperature near 15,000°K in a very thin sheath near the edge of the plasma, and that the center-line temperature is less than 15,000°K.

These observations are compatible with two other related physical characteristics of this plasma. The first proposed characteristic is that when effect caused by the laser is transferred to the plasma in a cylindrical sheath in the area of maximum electrical conductivity, which occurs in the area of maximum temperature. The second proposed characteristic is that a strong reverse gas flow in the center of the laser tube caused by reflection of the gas at relatively high velocity, is modified only slightly by the presence of the plasma. The existence of strong back-flow in the center of the laser tube requires the existence of very high temperatures in this area because of the high viscosities exhibited by plasmas whose temperatures are above 15,000°K.

The plasma is pictured therefore, having its maximum temperature existing in a thin cylindrical sheath near the outer limit of the plasma, with a strong reverse flow of relatively cool gases up through the



center of the plasma. These findings are contrary to the findings of T. B. Reed who concluded that the highest temperatures exist at the plasma center (Ref. 1: 223). The plasma investigated by Reed, was operated at a frequency of 4 megacycles at atmospheric pressure, using low gas flow rates, in a quartz tube with an outside diameter of 76 mm.

#### Operating Modes

The plasma was operated in four modes, as shown in Table I. As the study was originally conceived, Mode 1 was to be the standard mode for use in the analysis, and the other modes were to be different from Mode 1 in only one parameter. However, the plasma would not start in

Mode 1 with a plate voltage setting of 7.6 kilovolts (kv); and plasma operation in Mode 2 was possible with a plate voltage of 7.6 kv, so the higher plate voltage was used. Mode 1 was chosen as the standard mode because operation in this mode was the simplest. Laboratory techniques used in this study resulted from the experience gained while operating in Mode 1.

Table I  
Operating Modes

Mode	Plate Voltage (kv)	Gas (% by Volume)	Inner and Outside Diameter
1	7.6	100, N <sub>2</sub>	75-mm
2	8.2	100, N <sub>2</sub>	75-mm
3	10.1	100, N <sub>2</sub>	1.5-mm
4	8.2	53, N <sub>2</sub> 47, He	75-mm

Table 2. Operation in Table 2 was to show the effect of increasing the rf power available at a duty cycle of 100 . No particular difficulties were encountered during operation in this mode; however, power control, which is essential, was more critical at 30 dbm rf power than at 10 dbm. The duty cycle was increased to 50 percent in Table 2 and this is shown in Table 3.

[illegible][illegible]

Note 4. Operation in Note 4 was to show the effect of filtration on the separation with column. Filtration of near full-gal volume was desired, and operation with this filtration required a plate voltage of 2.2 kv to insure reliable operation. The mixture that was used in

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this mode was approximately 4" in diameter by volume. The plasma was started in pure argon and the helium was introduced after the duty cycle had been adjusted to 100%. The temperature of the plasma which was 47 helium was not very different from the temperature of a pure argon plasma. However, if the temperature were to appreciably increase, the filling time of the plasma would be increased, and the plasma density would be decreased.

### III. Discussion of Data

The discussion of the data is presented here under three headings; data reduction, data presentation, and data accuracies. In this manner, it is hoped that the reader will gain a feel for the problems involved using the experimental techniques outlined in this study.

#### Data Reduction

The recorded data were in the form of volts, amperes, and flow rates. These data were first converted into power units, kilowatts, and then tabulated as shown in Table II.

Table II  
Sample Power Measurements, Mode 3

Row	Gas Flow (scfh)	$\dot{Q}_w$ (kw)	$\dot{Q}_b$ (kw)	$\dot{Q}_c$ (kw)	$P_t$ (kw)	$P_i$ (kw)	$P_e$ (kw)
1	175	0.14		3.93	147.0	120.0	27.0
2	175		12.98	4.02	152.8	120.0	32.8

The symbols used in the table are defined as follows:

$\dot{Q}_w$  - The power measured from the clear water used to cool the plasma-generator.

$\dot{Q}_b$  - The power measured from the black water used to cool the plasma-generator.

$\dot{Q}_c$  - The power measured from the cooling water in the calorimeter.

$P_t$  - The plate power measured in the rf power supply when the plasma is operating.

$P_i$  - The plate power measured in the rf power supply when the plasma is not operating, or idling plate power.

$P_e$  - The excess plate power, which is the difference between  $P_t$  and  $P_i$ .

The first row of data was recorded during the clear water run and the second row recorded during the black water run. The difference in plate power between these two runs of 5.8 kw is larger than most differences recorded, but it serves to show the necessity of normalizing the data before any computation of the radial radiation power,  $Q_r$ , can be made.

The quantity  $Q_w$  is a measure of the power transferred to the walls by convection and that portion of the radiation absorbed by the clear water and the glass tubes. This portion of the radiation power was assumed negligible in comparison with either total radial radiation power, or convective power to the walls. The quantity  $Q_b$  is a measure of the sum of the power transferred to the walls by convection,  $Q_w$ , and the radial radiation power,  $Q_r$ .  $Q_r$  is radial radiation power that exists in the range of wavelengths for which Vycor, water, and Pyrex are transparent.

Note: The quantity  $Q_r$  will hereafter be referred to simply as radiation power. It is in fact a measure of radial radiation only, as the axial radiation power is absorbed by the top end-piece of the plasma-generator and the calorimeter. No attempt was made to measure the axial radiation power, but it is included in the measurement of  $Q_w$  and  $Q_c$ .

If we therefore subtract  $Q_w$  from  $Q_b$ , the difference should be  $Q_r$ . From Table II, the value for  $Q_r$  thus computed would be 3.84 kw. Implied in this computation is the assumption that all the additional power measured with the black water was radiation power, and no consideration was given to fact that the rf plate power was 5.8 kw higher during the black water run. This increase in plate power reflects an increase in rf power output of something less than 5.8 kw due to normal losses in

the rf power supply. In turn, there would be an increase in power transferred to the gas somewhat less than the increased rf power output due to normal coupling efficiencies between the rf coil and the plasma.

The problem, therefore, is to determine how much of the 3.14 kw is due to radiation, and how much is due to the increase in rf power output. An exact answer to this problem can be obtained by normalizing the  $P_{\text{eff}}$  and  $P_{\text{in}}$  before subtraction.

The data were normalized with respect to  $P_0$ . Table III lists the values for  $P_0$  for the different plate voltage settings. The  $P_{\text{eff}}$ ,  $P_{\text{in}}$ , and  $P_{\text{out}}$  are divided by  $P_0$  to produce a quasi-efficiency which will be called efficiency. We will refer to these as  $\eta_{\text{eff}}$ ,  $\eta_{\text{in}}$ , and  $\eta_{\text{out}}$ , respectively. Values for  $\eta_{\text{eff}}$  are plotted in Figure 17. Table IV is the result of normalizing the data in Table II.

Table III  
Idle Plate Power

Mode	Plate Voltage (kv)	$P_0$ (kw)
1	7.6	62.0
2	8.7	77.0
3	10.1	120.0
4	8.2	77.0

Table IV  
Sample Normalized Power, Mode 3

Gas Flow (scfh)	$E_w$ ( )	$E_b$ ( )	$E_c$ ( )	$E_T$ ( )	$\eta_T$ (kw)
175	33.8		14.55	5.8	1.57
175		30.6	12.25	5.8	1.90

$\bar{E}_p$  is taken as the difference between  $I_{p1}$  and  $I_{p2}$ , and is assumed to be unaffected by the different values of  $I_0$ . The validity of this assumption is open to doubt, but it appears to be a better first approximation than assuming that  $\bar{E}_p$  remains constant during the increase in  $I_0$ . The values for  $\bar{E}_p$  listed in Table II are found by multiplying  $\bar{E}_p$  by the appropriate  $I_0$ . This was done for the sake of comparison with the non-normalized value for  $\bar{E}_p$  of 3.9% in. It is also apparent from Table IV that two values for  $I_0$  can be obtained at each gas flow. Hereafter when a value is given  $I_0$ , whether it be in text, table, or graph, the value given will be the average of the two values of  $I_0$  for that gas flow. From Table IV, the value of  $I_0$  is 13.4% for a gas flow of 175 scfh.

The quasi-efficiency nature of the quantity  $\bar{E}$  was mentioned, without discussion, before.  $\bar{E}$ , as defined, is the percentage of excess plate power which goes to the plasma. The percentage of additional rf power which goes to the plasma would be of more interest to this study, but no means of measuring rf power was at hand. It is possible to say, however, that the amount of rf power available from this power source to operate the plasma is less than  $I_0$ , as it is not likely that all of this excess plate power is converted to rf power. Therefore, the values found for  $\bar{E}$  will be conservative estimates of the coupling efficiency between the rf coil and the plasma. Another of interest, in addition to power conversion efficiencies, is the manner in which the power that goes to the plasma is distributed between the wall, radiation,

and the calorimeter. After  $E_d$ ,  $E_p$ , and  $E_c$  are found, they can be summed to form a total effectiveness,  $E_t$ . Let the ratio of  $E_d$ , divided by  $E_t$ , be defined as  $R_d$ . Similarly, define  $R_p$  and  $R_c$ . These ratios show the distribution of power within the gas, as illustrated in Table V.

Table V  
Sample Power Ratios, Mode 3

Gas Flow (scfm)	$R_d$ (%)	$R_p$ (%)	$R_c$ (%)
175	63.8	10.9	25.3

#### Data Presentation

The data are presented in terms of the power coupling effectiveness,  $E$ , and the power distribution ratio,  $R$ , vs. gas flow in Figures 10 through 16. The points on the  $E_d$ ,  $E_p$ , and  $E_c$  vs. gas flow graphs (Fig. 10 and 12) were obtained by normalizing  $E_d$ ,  $E_p$ , and  $E_c$  with respect to  $E_c$ . The curves on these graphs represent the best fit to the data points by a second order (parabolic) curve. However, there is good argument for use of a third order (S-shaped) curves for  $E_b$ , Mode 2, and for  $E_d$ , Modes 2 and 3, based on the number of data points and their distribution. The type curve chosen to represent a series of data points should be based upon the exactness to which each data point can be located, as well as to the number and distribution of the points. If high confidence in the location of each data point is justified, a curve which closely fits all the data points can be drawn. If, however,



the possible variation in the exact location of a data point is large, then a lower order curve which tends to average out the point location uncertainties is more reasonable. The exact locations of the data points for  $E_w$  and  $E_b$  are not known with sufficient accuracy to justify more than a second order curve.

The feet attached to each end of these curves show the possible vertical displacements of the data points based upon the probable error in reading the coolant temperatures of plus or minus one degree Fahrenheit. These vertical displacements are essentially constant for all data points along that curve, and this display method was chosen over attaching the feet to each data point to prevent excessive cluttering of the graphs.

After the curves for  $E_b$ ,  $E_w$ , and  $E_c$  were plotted, the difference between the  $E_b$  and  $E_w$  curves was drawn as the  $E_r$  curve (Fig. 11), and the sum of the  $E_b$  and  $E_c$  curves was drawn as the  $E_t$  curve (Fig. 13). The data dispersion which is inherent in the process of subtracting at each data point, and then plotting, is shown quite well in the plots of the data for  $E_r$ . The data points shown result from the subtraction of  $E_w$  data points from  $E_b$  data points. The subtraction technique will always produce this type of dispersion whenever the data are not perfectly smooth. The probable vertical displacement of points on the  $E_r$  curves was taken as  $(2)^{1/2}$  times the average displacements for the  $E_b$  and  $E_w$  curves since these displacements are close to being equal.

The curves for  $R_w$ ,  $R_r$ , and  $R_c$  result from dividing the  $E_w$ ,  $E_r$ , and  $E_c$  curves by the  $E_t$  curve. In this manner, the normalizing quantity

$P_0$  is eliminated, and the resulting quotients,  $Q_w/Q_t$ ,  $Q_r/Q_t$ , and  $Q_c/Q_t$ , are the power distribution ratios,  $R_w$ ,  $R_r$ , and  $R_c$  (Fig. 14, 15, and 16).

#### Data Accuracies

The only significant source of error in the data results from the low accuracy to which the coolant temperature rises can be determined. By reading the deflection of the center of the temperature trace to the nearest 1/40-in., the probable error in temperature measurement is approximately plus or minus one degree Fahrenheit. The following example illustrates the consequence of such an error.

For a typical coolant flow of 2500 pounds per hour, an error of plus or minus 0.732 kw may be expected in the value for  $Q_w$ . The resultant errors in  $E_w$ , from errors in power of this size, range from plus or minus 2.5% to plus or minus 0.9%. That is to say  $E_w$  equals 40% plus or minus 2.5%. For  $E_b$ , the errors due to inaccurate temperature measurement, range from plus or minus 2.2% to plus or minus 0.8%, which are slightly less than errors for  $E_w$  due to the lower black-water flowrate. The errors in  $E_r$  will contain the errors in  $E_w$  and  $E_b$ . Since the errors in  $E_w$  and  $E_b$  for a particular operating mode and gas flow are approximately equal, the error in  $E_r$  was taken as the  $(2)^{1/2}$  times the numerical average of the errors for  $E_w$  and  $E_b$ . The range of errors thus computed for  $E_r$  are from plus or minus 3.3% to plus or minus 1.2%. Except for some variations in coolant flowrates, the errors in  $E_w$ ,  $E_b$ , and  $E_r$  due to an error of plus or minus one degree Fahrenheit, are inversely proportional to the normalizing quantity,  $P_0$ . Other errors

result from the accuracy to which the coolant flowmeters, plate voltmeter, plate ammeters, and gas flowmeters can read, and from the failure to remove all of the power from the gas in the calorimeter.

The two plate ammeters can be read to the nearest 0.1 ampere, and the plate voltmeter can be read to the nearest 0.1 kv. The inherent error here is plus or minus 0.0035 kw which is insignificant when compared with the lowest value of  $P_0$ , which is 27 kw.

The Alcoa flowmeters are stated to be accurate within five percent, and they can be read to the nearest one scfh. It is assumed that any inaccuracies in the flowmeter are distributed over the whole range of the flowmeter. This type error will be shown as a scale error on the graphs, without appreciably changing the general appearance of the curves. The inaccuracy in reading the flowmeter would show as a horizontal displacement of a data point on the graph, however, a horizontal shift of one scfh would be hard to detect on the scale of 50 scfh per inch.

The largest amount of power remaining in the gas as it left the calorimeter was on the order of 0.03 kw. Had the calorimeter been totally effective, this power would add to  $Q_c$ . Since the smallest value for  $Q_c$  was 2.42 kw, the error in neglecting the power remaining in the gas is acceptable.

The water flowmeters could be read to the nearest five pounds per hour, or to within two and one-half pounds per hour. This error in coolant flow can lead to an error in power measurement up to 0.06 kw

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depending upon the coolant temperature rise. The largest coolant temperature rises were in conjunction with power measurements on the order of 30 kw, so that this error is also negligible.

#### IV. Results and Conclusions

Before presenting the results and conclusions, it is necessary to fix in the mind of the reader exactly what was measured during this study, and what the purposes of the study were.

The quantities  $Q_w$  and  $Q_b$  represent the power transferred to the coolant as it passes through the plasma-generator. The quantity  $Q_c$  represents the power transferred to the coolant in the calorimeter.

$Q_w$  is composed of three terms; a wall loss term, a radiation term, and a duct loss term. The wall loss is the power transferred by convection to the wall in the area of heat addition to the plasma. Since the plasma extends up to the injection plate, some wall loss is experienced there also. The radiation term is composed of the radiation absorbed by the coolant, the outer Pyrex tube, the inner Pyrex tube, and the top and bottom end-plates. The duct loss term represents power transferred to the wall which was available in the gas flow as enthalpy after the gas left the area of heat addition.

$Q_b$  is composed of the same terms as  $Q_w$  with an additional radiation term. This additional term represents the radial radiation power absorbed by the black water.

$Q_c$  is composed of two terms. The first term represents the power available in the gas flow as enthalpy after the gas leaves the plasma-generator. The second term represents the radiation from the plasma which is absorbed in the calorimeter. For the most part, this radiation

is axial radiation, but at high gas flow in small diameter tubes, the visible plasma could extend down into the calorimeter, in which case some radial radiation would also be measured.

The definitions for  $Q_r$  and  $Q_t$  need not be further expanded.  $Q_r$  remains the difference between  $Q_b$  and  $Q_w$ , and represents the difference between the total radial radiation and that portion of radial radiation which is absorbed by the plasma-generator, clear water, and the calorimeter should the plasma extend that far down. The total power transferred to the gas,  $Q_t$ , remains the sum of  $Q_b$  and  $Q_c$ .

The normalizing quantity,  $P_0$ , is the difference between a varying total rf power supply plate power,  $P_t$ , and the constant value of idling plate power,  $P_i$ . When a constant duty cycle is chosen, no control can be exerted on  $P_t$ , as the rf power supply automatically adjusts  $P_t$  in response to the load placed upon it. Since  $P_0$  differs from  $P_t$  by a constant, the variation of  $P_t$  with gas flowrate can be deduced from the plot of  $P_0$  vs. gas flow (Fig. 17). Refer to Table III for values of  $P_i$ .

The normalized quantities,  $E_w$ ,  $E_r$ , and  $E_c$  represent a percentage of  $P_0$ , and therefore show how much of  $P_0$  was effectively transferred to the wall, to radiation, and to the calorimeter. When each of these characteristics is divided by their sum,  $E_t$ , the ratios  $R_w$ ,  $R_r$  and  $R_c$  are obtained. These ratios show the percentage of the total power transferred to the plasma that goes to the wall, to radiation, and to the calorimeter.

In general,  $E_z$  did not vary greatly with gas flow (Fig. 13). Therefore, if either  $E_r$ ,  $E_\theta$ , or  $E_c$  shows a strong variation, one or both of the other parameters must make compensating variations. Further, the relative constancy of  $E_z$  insures that increases or decreases in  $E_r$ ,  $E_\theta$ , or  $E_c$  are reflected by corresponding increases or decreases in  $R_r$ ,  $R_\theta$ , or  $R_c$ . For this reason, the results and conclusions will be discussed in terms of  $E_r$ ,  $E_\theta$ ,  $E_c$ , and  $E_z$  only.

The objectives of this study were (1) to operate a stable plasma at atmospheric pressure at 400 kc with a sustained high-power operation capability, (2) to determine the temperature profile of the plasma as a function of the plasma radius,  $T(r)$ , (3) to measure the power transmitted to the plasma, and (4) to determine parameters important to the energy coupling mechanism.

#### Plasma Operation

Using the techniques described in this study, a stable plasma was operated at 400 kc at atmospheric pressure. No endurance runs were made, however, the plasma has been continuously operated for forty minutes during some data runs which included peak plasma powers up to 52 kw. With a modified injection plate to prevent injection plate damage, and heat resistant seals to prevent seal deterioration, the plasma is believed capable of continuous operation at the 50 kw power level at gas flows above 100 scfh, in a 75-mm Vycor tube. Stable operation of the plasma was concluded on the basis of apparent constant plasma geometry, and stationary values of coolant temperature indications during operation at constant gas flow.

Temperature Profile

Although temperature profile measurements were not complete, the existence of a temperature of  $15,000^{\circ}\text{K}$  near the outer surface of the plasma was verified, and a model temperature profile was deduced. The deduced temperature profile shows the highest temperatures occurring in a thin cylindrical shell near the outer surface of the plasma, and relatively cooler center-line temperatures existing in a reverse gas flow.

Power Measurements

The techniques used to measure power were only partially successful. The margin for error in determining the coolant temperature rise was unacceptable for so critical a measurement. This fault coupled with the shift in  $P_0$  between the clear water and black water runs, led to excessive data dispersion which in turn prevented obtaining point-by-point radiation power values by subtraction of the point values for  $Q_w$  and  $Q_b$ .  $Q_w$  and  $Q_b$  were normalized with respect to  $P_0$  and the results plotted as  $E_w$  and  $E_b$  vs. gas flow in scfh. A smooth curve for  $E_w$  was then drawn and subtracted from the smooth curve drawn for  $E_b$ . This yielded smooth curves for normalized radial radiation power,  $E_r$ . The usefulness of radiation values obtained in this manner rests on the validity of the averaging processes inherent in normalizing data and plotting smooth curves. In consideration of the limitations imposed by possible data accuracies and experimental techniques used in this study, the information displayed on all graphs should be viewed as



first approximations of actual values and trends.

The black water technique as applied in this study is very useful as a means of determining total plasma power. Better measurements of radiation power would be possible with the use of an improved black water which did not leave deposits on the inner tube. This innovation is discussed under "Recommendations". With the use of an improved black water, this technique of measuring radiation power should yield useable radiation power data without the necessity of first normalizing the data.

#### Coupling Parameters

The controlled parameters were rf power supply plate voltage, inner Vycor tube diameter, gas composition, and gas flow, however, other implicit parameters were present. The implicit parameters appearing in this study are plasma pressure, vortex strength, rf power supply plate power, and plasma length and diameter. No control can be exerted over these parameters, as they are the natural consequences of varying the controlled parameters.

Conclusions concerning a coupling parameter must be supported by a reasonable quantity of data pertinent to the effects of that parameter. The preponderance of information gathered in this study directly concerned gas flow. For this reason, the effects of varying gas flow are well described. The effects of varying gas composition, inner tube diameter, and plate voltage cannot be described nearly as well due to the meager investigations made of each of these parameters.

Direct comparisons of the operating modes which contain these parameters as variables can establish a trend which would have some short range validity, but any long range projections made on the basis of these limited comparisons are of doubtful validity.

Gas Flow. The effect of increasing gas flow on all operating modes is similar, but somewhat varying in degree. For instance, a sharp decrease in  $Z_p$  is noticed with an increase in gas flow for Modes 1, 2, and 3; but Mode 4 exhibits only a slight decrease in  $Z_p$ . In general, the decrease in wall loss and radiation characteristics and the increase in the calorimeter characteristics with increasing gas flow can be attributed to the decrease in plasma diameter which occurs with increasing gas flow. Some lengthening of the plasma tail-flame is also noted with increased gas flow, but no significant increase in length of the highly luminous portion of the plasma was observed. As the plasma contracts, at high gas flows, wall losses are inhibited by the increased separation between the plasma and the walls, and the effective volume of radiating plasma is decreased, thereby reducing radiation losses. The reduction in radiating volume apparently offsets any tendency to increase radiation power through possible increased plasma temperatures. In the absence of temperature measurements to the contrary, it is believed that plasma temperature very likely decreases with the increasing gas flow due to the decrease in energy coupling to the restricted plasma volume.

The reduction of wall losses and radiation losses at higher gas

flows is reflected by an increase in power carried to the calorimeter by the flowing gases.

Gas Composition. The only gas used other than argon was a mixture of argon and helium. The mixture used was approximately 47% helium by volume, or about 8.9% helium by weight. This dilution of pure argon led to marked differences between the results of Mode 1 and Mode 2. The increase in wall loss characteristics and the decrease in radiation loss characteristics are respectively believed to be the result of the higher thermal conductivity and lower emissivity of helium. The calorimeter characteristics for these two modes are nearly equal, which suggests that the decreased radiation losses were offset by equivalent increases in wall losses.

Plate Voltage. The effects of increasing plate voltage appear in the comparison of Modes 1 and 2. The changes experienced by raising the plate voltage were the least predictable of all changes resulting from varying the other parameters. It was earlier observed that an increase in rf power output increased the diameter of the plasma. During any data run it was also observed that as the diameter of the plasma increased  $E_t$  increased. These two bits of information seemed to point the way toward an increased coupling effectiveness at higher plate voltage settings. It was predicted that the higher rf power output, which would accompany the higher plate voltage setting, would increase the plasma diameter which would in turn increase  $E_t$ . The effect on  $E_t$  was just the opposite;  $E_t$  decreased.  $Q_w$ ,  $Q_r$ , and  $Q_t$ , however, increased in Mode 2, but these increases were obtained at relatively higher increases

in  $P_0$ , so that  $E_1$ ,  $E_2$ , and  $E_3$  decreased in Mode 2. The most unexpected result was that  $Q_0$  for Mode 2 was less than  $Q_0$  for Mode 1, for an increase in all power measurements was expected because of the increased rf power output.

No explanation of the decrease in  $E_1$  is offered. An examination of Figure 8 shows a decrease in electrical conductivity of an argon plasma at temperatures from 22,000K to 25,000K. A decrease in conductivity of the plasma could account for the decrease in  $E_1$ , but the existence of temperatures on the order of 22,000K is ruled unlikely, although a temperature profile at this power level was not attempted. The decrease in  $Q_0$  is possibly due to increased energy losses to the wall since the highest gas temperatures occurred closer to the walls. Further work is needed to clarify the apparent contradictions that occurred during Mode 2 operation.

Inner tube diameter. The variations in plasma characteristics resulting from using a smaller diameter inner tube in Mode 3, show the effects of constriction of the plasma, and thereby reducing the energy coupling and the effective radiation volume of the plasma, and the effect of the close approach to the wall by the plasma. The total effective coupling is low due to reduced energy coupling. The radiation characteristics are low due to the small radiation volume and probable lower plasma temperature, and the wall loss characteristics are high due to the close proximity of the plasma to the wall. The calorimeter characteristics are also noted to be high, but these values

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are questionable. The possibility that the plasma extended down into the calorimeter during Mode 3 operation was previously mentioned. This event would result in measuring a certain amount of radial radiation in the calorimeter, and suggests that the values shown for the calorimeter characteristics are too high, and that the values shown for radiation characteristics accordingly are too low.

## V. Recommendations

### General

The conclusions presented here were based on a study which just scratched the surface of the research needed for the proper understanding of the phenomena of the induction-coupled plasma. These conclusions represent the best that the present investigation has to offer.

The main areas for improvement and continued study brought out by this study are (1) the plasma-generator, (2) the coolant temperature measurement, (3) plasma temperature measurement, and (4) radiation power measurements.

An additional parameter which is available through the use of the duty cycle control on the power supply should be studied. Duty cycles less than 100% will have an important bearing on the efficiency of an induction-coupled plasma used as a gas heater.

### Plasma-Generator

Gas Injection Plate. The present gas injection plate with eight injection holes on a two-inch diameter circle offers no flexibility to gas injection, and the center of the plate is subjected to severe heating at high power operation. To add flexibility to gas injection, it is recommended that the injection system use two sets of injection holes drilled on different diameters. Each set of holes would be of different size and be supplied gas through independent gas manifolds.

This arrangement would allow the selection of different vortex strengths at the same total gas flow. In this manner, the effects of vortex strength could be shown. The results of this experiment could be presented as illustrated in Figure 18. The curves would be lines of constant gas flow. The left most point would represent 100% of the gas issuing from the manifold with the larger holes, and the right most point would represent 100% of the gas issuing from the manifold with the smaller holes.

A method for eliminating the heat loads on the injection plate was suggested by L. Soehren. He suggested that a small amount of gas injected axially from the center of the injection plate would prevent the plasma from contacting the plate. As an extension of this idea, it might very well be possible to accurately position the tor of the plasma by varying the axial gas injection which would control the reverse gas flow. Preventing the plasma from contacting the injection plate will allow operation at higher powers without contamination of the plasma by material from the injection plate.

Tube Diameters. The manner in which the power coupling increases as the plasma expands suggests that the ratio of plasma diameter over rf coil diameter ( $D_p/D_c$ ) is a parameter which should be studied. Studies should be made using larger diameter tubes, but keeping the same waterjacket thickness, or possibly reducing the waterjacket thickness, in order to increase  $D_p/D_c$ .

Start-up Mechanism. A large percentage of tube damage and breakage that occurred during this study could be directly attributed to "hot starts" using the vacuum start technique. T. B. Reed used an inductively heated piece of a rod or refractory fire loop to start the plasma at low gpm pressure (ref. 7: 21). The breakdown potential of the insulating oil in the tank was not sufficient to allow ignition of the plasma by the fire loop. Starting the plasma at atmospheric pressure would prevent the tube damage experienced during vacuum starts, and would also eliminate the need for a vacuum system. A means of heating the inductively heated rod or refractory fire loop through the vacuum tank would be devised for starting purposes.

Seals. Seals for the inner and outer tubes were provided by standard O-rings. O-rings at the bottom of the inner tube are subjected to severe heating, and cannot be reused. The O-rings are heated by radiation and conduction from the inner tube. Should the plasma exit the outer nozzle a few minutes at full power, these bottom seals almost certainly will have to be replaced before a sufficient vacuum for re-starting is reached. A higher temperature capability of all the rubber seals that O-rings are made of, silicone rubber or Viton, or at least one, this problem.

Water Jacket. The space between the inner and outer tubes for a large part determines the water flow necessary to prevent local boiling next to the inner tube. Reducing this space, by proper selection of tube diameters, leads to smaller water flow requirements for the purpose of reducing local boiling. Reducing the water flow in turn reduces



the error in power measurements due to water temperature determination accuracy. If the waterjacket is made too thin, however, the black water technique for total power measurement may not be effective. In general though, smaller water flowrates, and higher temperature rises lead to better accuracies for power measurements, and therefore, a thin waterjacket should be considered.

#### Coolant Temperature Measurements

Coolant temperature measurements are very critical to power measurements, especially at high coolant flows. Temperature measurements accurate to the nearest one-half degree Fahrenheit would more nearly equal the magnitude of error in power measurements resulting from temperature inaccuracies to the magnitude of error resulting from water flow inaccuracies. Reducing temperature inaccuracies beyond this point will yield little in overall accuracy, and therefore become luxuries. At the least, temperature measurements should be accurate to the nearest degree Fahrenheit.

#### Plasma Temperature Measurements

An accurate knowledge of the temperature profile of an induction-coupled plasma is essential to the understanding of the basic phenomenon of induction-coupled plasmas, and to the development of theories to explain this phenomenon.

At present, W. T. Braun of the Physics Branch, Aeronautical Research Laboratory, and C. Grabner, Chief of Analysis Branch, Digital Computation Division, Aeronautical Systems Division, are developing a

computer program which will yield a spectral line intensity profile,  $J(r)$ , from an observed  $N(x)$ . The computer program will be applicable to any measurements for which axial symmetry can be assumed. When the program is established, the computer will fit an even ordered polynomial ( $a_0 + a_2x^2 + a_4x^4 + \dots + a_{2n}x^{2n}$ ) to the observed data to obtain an analytical expression for  $N(x)$ . It will then differentiate  $N(x)$  with respect to  $x$ , substitute  $N'(x)$  into the integral equation, Eq (1), and perform the integration to obtain  $J(r)$ .

When this valuable tool is available to make multiple temperature profile determinations practical, a series of test runs in the pattern of this study should be made to determine the parameters which effect the maximum temperatures attainable, and the radius at which these maximum temperatures occur.

#### Radiation Power Measurements

Radiation power measurements in this study were hindered by two basic faults, other than inaccurate temperature measurements. The time difference between the clear water and black water readings is one fault, and the other fault is the inability to reproduce the plasma, as evidenced by the different values of  $I_0$  which occur at the same gas flow during the same data run. Ideally, all measurements are made simultaneously so that there is no time difference and no non-reproducibility problem.

Since plasma power is not time dependent while operating at a constant gas flow, measurements can be made at different times and still be valid if they do not depend upon reproducibility. This condition is satisfied by leaving the gas flow constant and switching the coolant supply between clear and black water to get measurements of both  $q_w$  and  $q_b$ . However, the black water used in this study deposited on the inner tube, and no clear water measurements could be taken after black water was once used. Therefore, an opaque coolant which does not deposit on the inner tube should be found for use in this radiation measurement technique.

A possible method for obtaining simultaneous power measurements was suggested by R. Winkerson, Physics Department, Air Force Institute of Technology. He proposed that the amount of radiation falling on a radiometer at some fixed distance from the plasma should be compared with the radiation measurements made by switching to black water without changing gas flow, to determine if the two radiation measurements are in some manner proportional. Using the present black water supply, this method entails cleaning the plasma-generator, between test runs. If a proportionality exists, then the radiometer should be carefully calibrated by a series of runs, so that subsequent radiation measurements can be made using the radiometer. The ability to obtain simultaneous power data is well worth the effort to calibrate the radiometer, therefore, tests for proportionality should be made.

### Energy Balance

An energy balance on the plasma was not performed because no measurements of total electrical power transferred to the plasma could be made. There is a relative simple method available to measure the electrical power absorbed by the plasma, but it requires additional instrumentation on the rf power supply. This method was suggested by Taylor and Hastings (Ref. 3: 1371). The additional instrumentation required is an rf ammeter in the circuit with the rf induction coil, and water flowmeters and thermocouples in the cooling system for the triodes in the rf power supply.

The total electrical energy supplied to the triodes can be measured with direct-current meters. The energy lost in the triodes is given off as heat and can be measured by reference to cooling water temperature rise and water flow. The energy not lost in the triodes is converted to rf energy output.

To obtain a measure of rf energy transferred to the plasma, the power supply is first operated in the absence of a plasma at some set value of rf current on the rf ammeter in the induction coil circuit. Total electrical energy to the triodes and total triode losses are then measured as previously explained. The difference between these values is the rf energy losses which occur at that rf current. The power supply is next operated in the presence of a plasma, at the same rf current. The total triode energy input and losses are measured as before. The rf energy losses at this rf current were previously determined. The rf energy losses are added to the triode losses which

occurred on the second run, and this sum is then subtracted from the total energy supplied to the triodes on the second run. This difference is the energy which is transferred to the plasma.

By knowing the rf energy supplied to the plasma, a proper energy balance can be made. An energy balance is deemed necessary to validate the measurements made on the plasma by the techniques used in this study.

### Supersonic Heating

The possibility of adding heat to the air in the supersonic region of a hypersonic wind tunnel by a rf induction-coupled plasma, was mentioned in the introduction. However, plasma operation in gases with high linear velocities is unstable because the plasma cannot propagate fast enough upstream. In the vortex-stabilized plasma, ionized gas is blown upstream by the back-flow. This feedback system continuously supplies the ions necessary to maintain coupling between the rf induction coil and the plasma.

Stabilization by vortex flow in hypersonic wind tunnels cannot be considered, because it disrupts the gas flow. A schematic presentation of a stabilization scheme is shown in Figure 19. This scheme involves a constant supply of electrons being injected into the gas flow near the throat of the wind tunnel. These electrons are carried downstream, by the fast moving gases, into the plasma coupling area where they couple with the rf induction coil, and thereby stabilize the plasma. As the electrons move downstream past the plasma area they are returned to ground, leaving a neutral gas behind.

The electrons can be generated in a typical electron-dynamic ion-production method. For negative ion production, the corona discharge needle is given a high negative charge, just short of breakdown potential. The positive ions created near the needle point are attracted to the needle, whereas the negative ions are attracted to the nearby ground. Before the electrons can reach ground, however, they are carried downstream through the plasma discharge area by the gas stream.

This stabilization scheme seems feasible. There is no doubt that the negative-ion stream can be generated; but only experimentation will show if this ion stream will couple with the induction coil, and if the plasma thereby generated can be confined to a volume small enough to prevent destruction of the tunnel walls. If coupling occurs without damage to the tunnel wall, the usefulness of this heat addition method is limited only to the extent to which the plasma experiences a breaking effect caused by interaction between induction currents in the plasma and the field of the rf coil.

This heat addition system in the supersonic flow section of a hypersonic wind tunnel appears feasible, and should be checked by experimental means.

#### Duty Cycle as a Parameter

A duty cycle control on the rf power supply allows selection of any duty cycle desired between 0% and 100%. For any particular plate voltage setting, this allows selection of any plate power from zero to the maximum attainable on that plate voltage setting. Consequently,

with a prior knowledge of idling plate power,  $P_0$ , for that plate voltage setting, a particular value of  $P_0$  can be selected exactly by use of the duty cycle control.

When the rf power supply is operated at a duty cycle less than 100%, the rf power is emitted in pulses at the rate of 360 per second. The duty cycle percentage corresponds to the length of these pulses. A duty cycle of 36%, for example, yields power pulses whose duration are 0.001 second, and which occur at a rate of 360 per second. During any second then, the rf power is emitted for 0.36 second.

The pulsing nature of this power supply is of considerable importance in the use of an inductively-coupled plasma as a gas heater, such as for the heating of cathodes. One of the characteristics of plasmas, when formed in a direct-current arc, is that they are so viscous they defy efforts to blow them through the arc channel. This reduces the effectiveness of heating cathodes by electric arcs. The shortcoming of arcs can be circumvented in a pulsed induction-coupled plasma, because instead of relying on heating the cold gases by moving the cathode through the plasma, the plasma propagates through the cold gases. High speed photographs taken of a plasma operating at a duty cycle of 50% clearly show the pulsing nature of the plasma. When the power pulse ends the plasma rapidly cools rapidly, and the radiating plasma gradually shrinks toward the center of the tube. When the next power pulse occurs, it couples with the remaining conducting gas, and the plasma gradually swells to normal size. The pulsing of the plasma is not visible to the eye, and normal size refers

to the size of the plasma seen by the eye. It is proposed that this pulsing action of the plasma more effectively heats the gas than operation of the plasma at a duty cycle of 100, because wall losses and radiation should decrease due to pulsing the power. A series of tests would be run at the same gas flow and  $P_0$  on the nine possible plate voltage settings to confirm or deny this proposal.

### Summary

Very little information is available on induction-coupled plasmas to date. This study is the only work known to the author which is available on induction-coupled plasmas operating below the megacycle range. As it was so simply and in this study is versatile enough to test the ingenuity of the investigator to use it. It is probable that sufficient information is available to investigate plasmas in pure gases other than air or air at atmospheric pressure. If a plasma-generator is developed to contain it, the studies which would be conducted on induction-coupled plasmas are so numerous that it would be desirable to outline a systematic, long-term program of investigation. This study has established the general characteristics of a high-power induction-coupled plasma-generator, and has revealed a number of experimental difficulties which must be considered. Thus a comprehensive program of investigation may now be confidently undertaken.



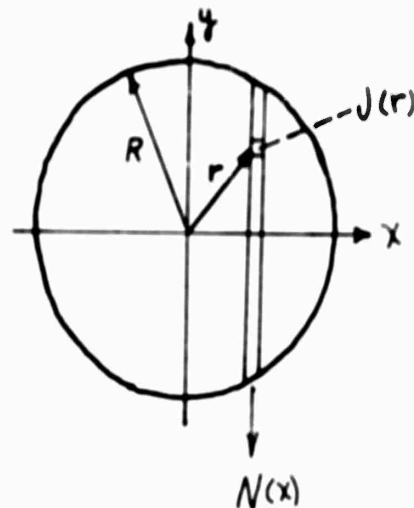
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2. Reed, Thomas B. "Induction-Coupled Plasma Torch". Journal of Applied Physics, 32:821-824 (1961).
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## Appendix A

Abel's Integral Transformation

The transversally observed radiance of the plasma image,  $N(x)$ , is inverted to the radiant intensity,  $J(r)$ , in the following manner.



$$N(x) = 2 \int_0^y J(r) dy$$

But,

$$y = \sqrt{r^2 - x^2}$$

And,

$$dy = \frac{r dr}{\sqrt{r^2 - x^2}}$$

Therefore:

$$N(x) = 2 \int_x^R \frac{J(r) r dr}{\sqrt{r^2 - x^2}}$$

This is Abel's integral, which inverts analytically to form

$$J(r) = -\frac{1}{\pi} \int_r^R \frac{N'(x) dx}{\sqrt{x^2 - r^2}}$$

The prime indicates differentiation with respect to  $x$ .

Figures

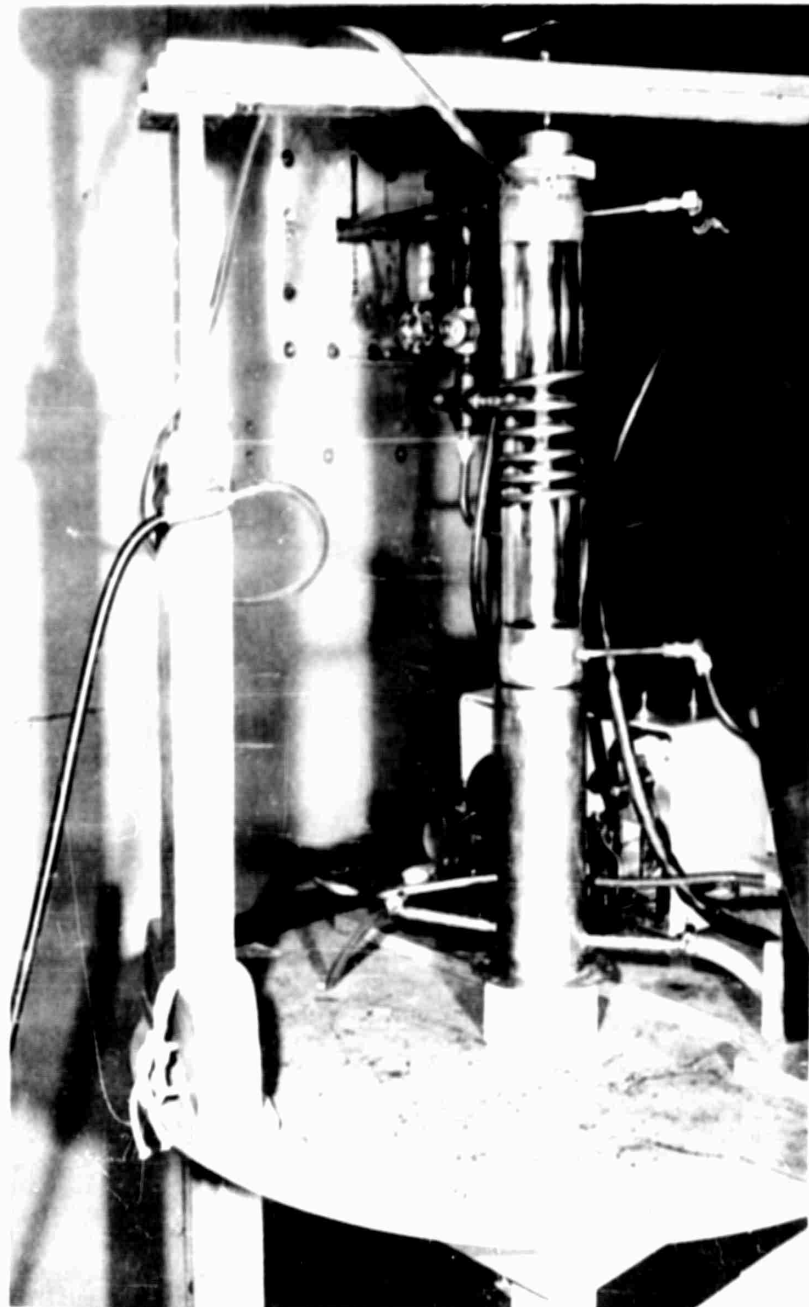


Fig. 1  
Plasma-generator with  
clear water coolant

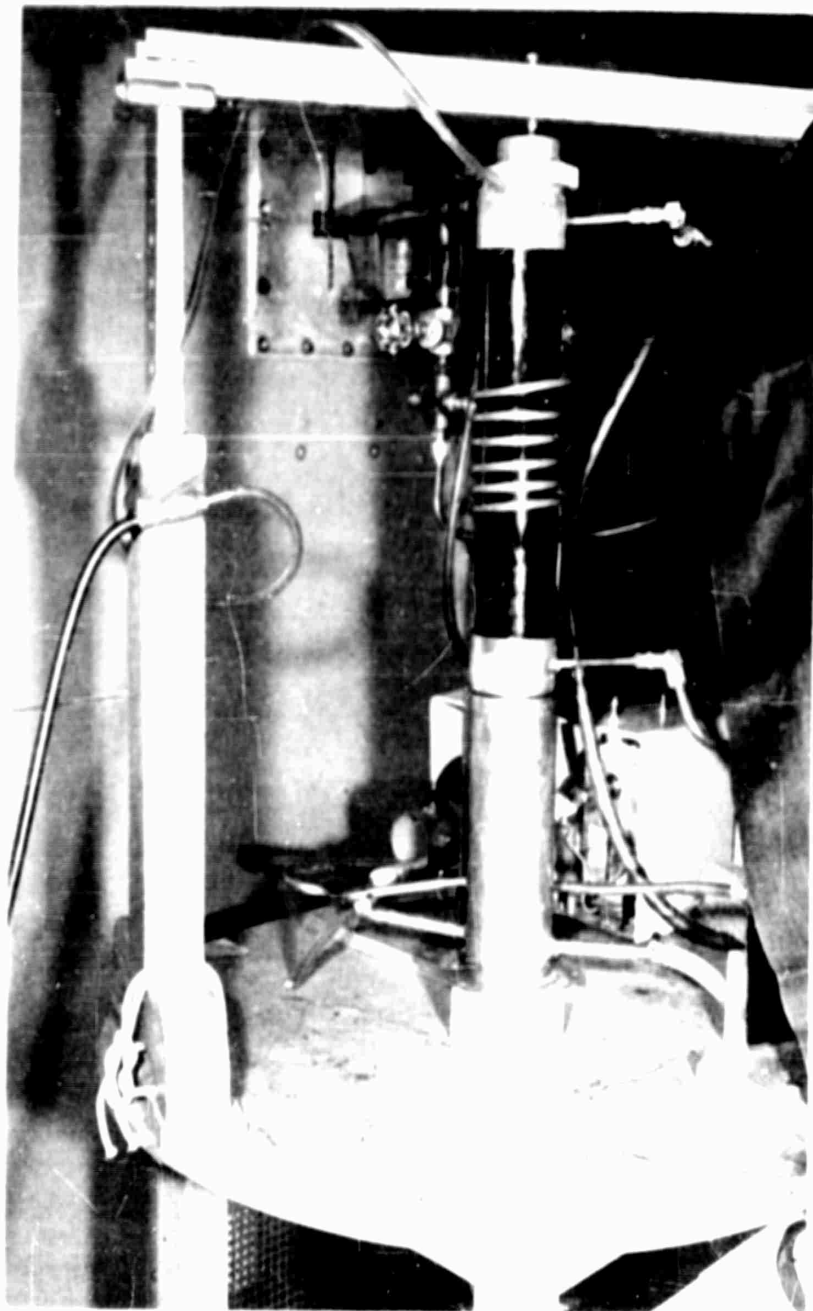


Fig. 2  
Plasma-generator with  
black water coolant

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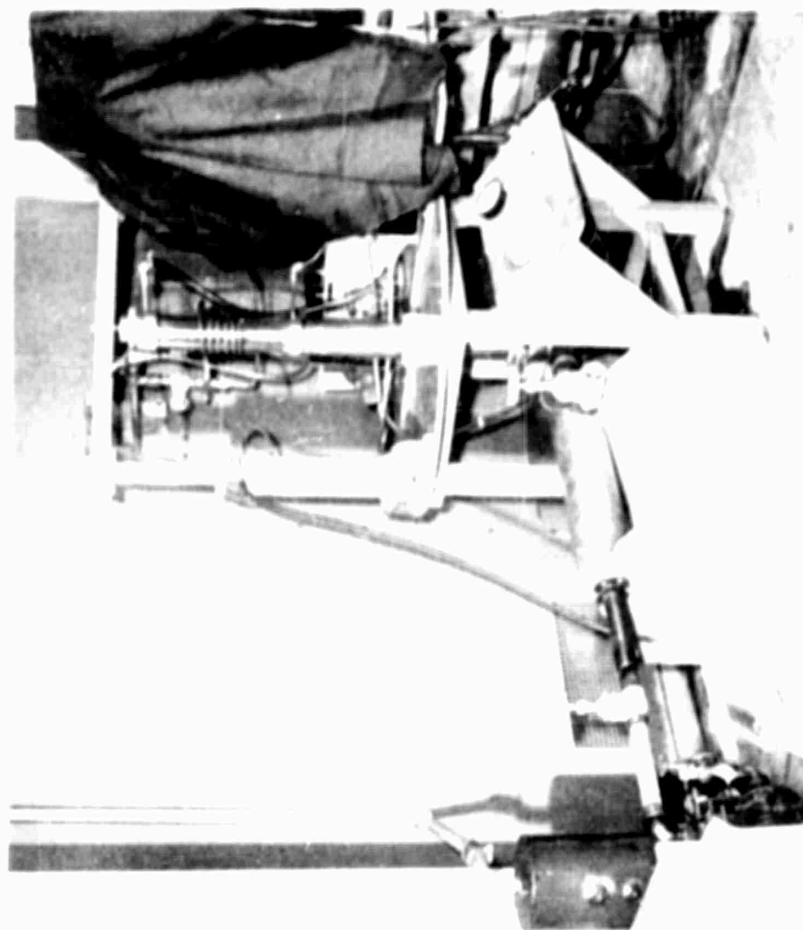


Fig. 3  
Experimental apparatus

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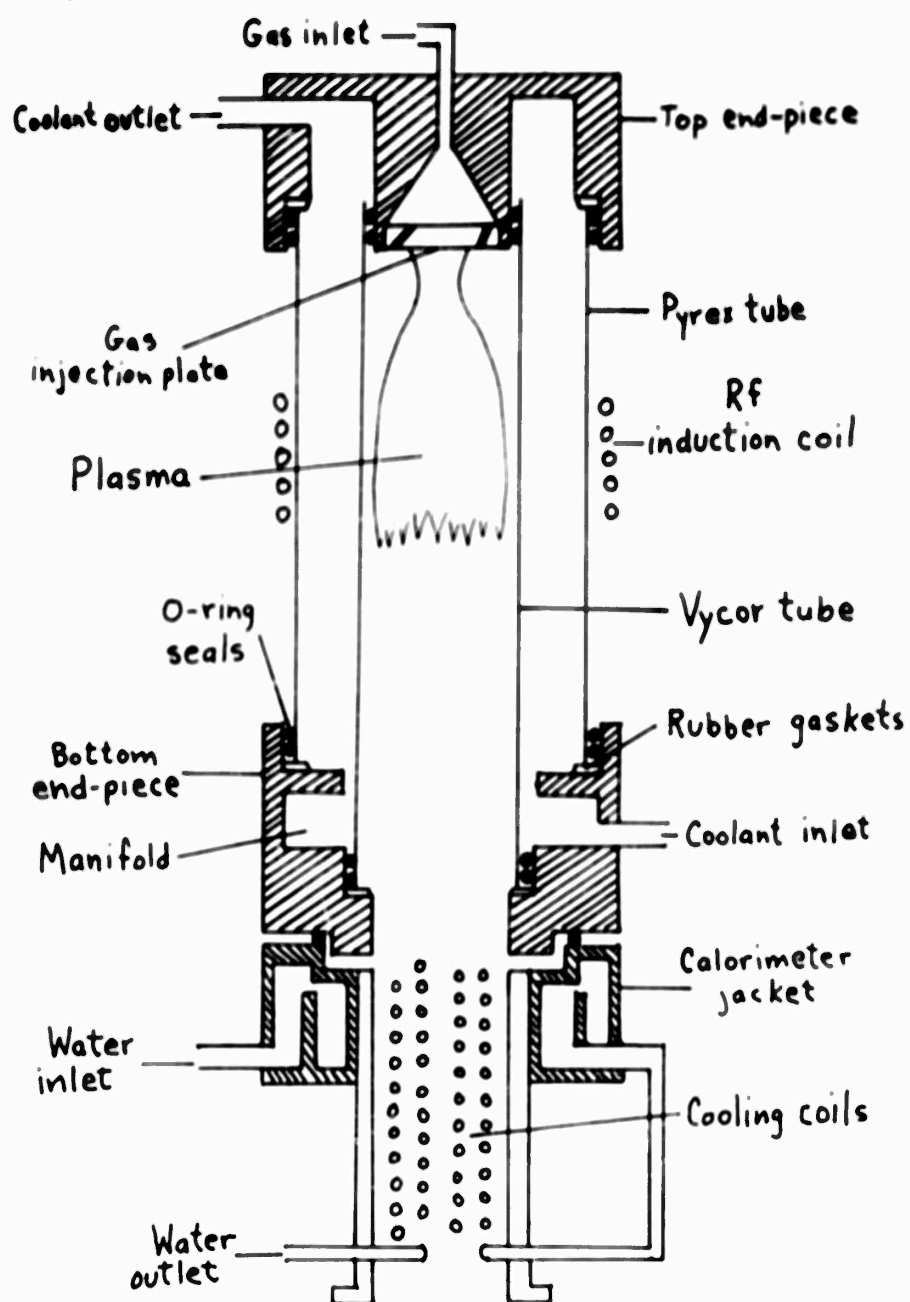


Fig. 4  
Schematic of plasma-  
generator and calorimeter

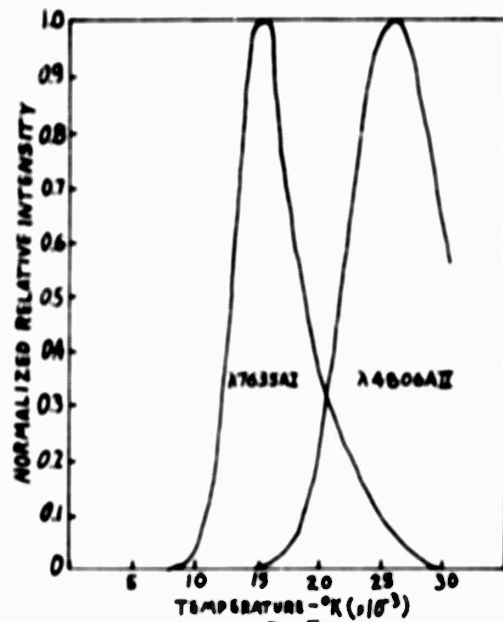


Fig. 5

(From Ref 1:617)

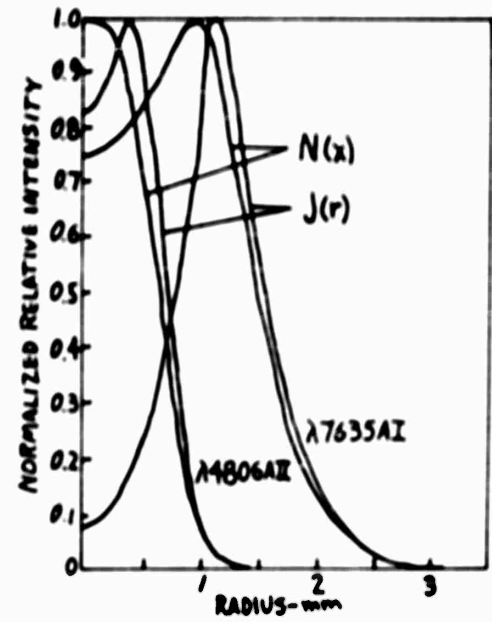


Fig. 6

(From Ref 1:616)

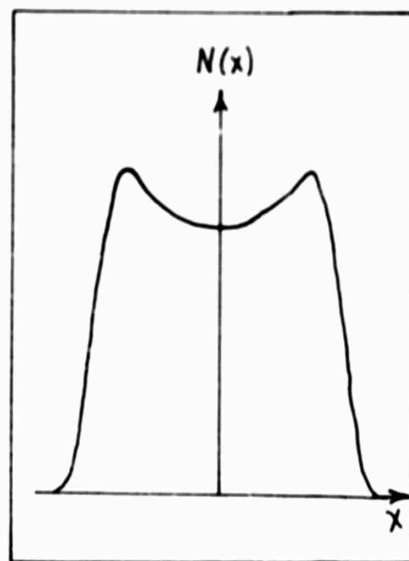


Fig. 7

Typical observed intensity  
of  $\lambda 7635 \text{ AI}$

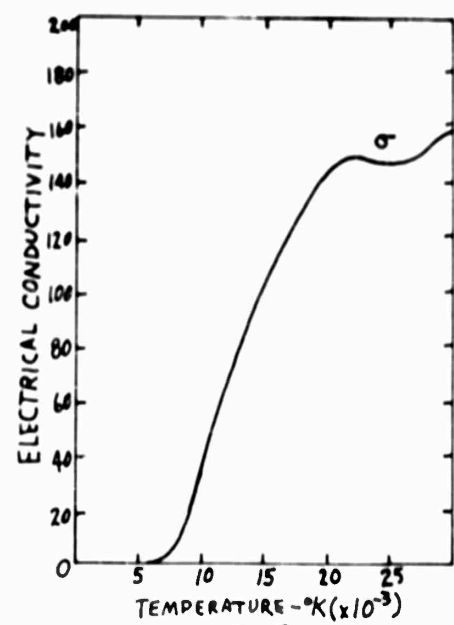


Fig. 8

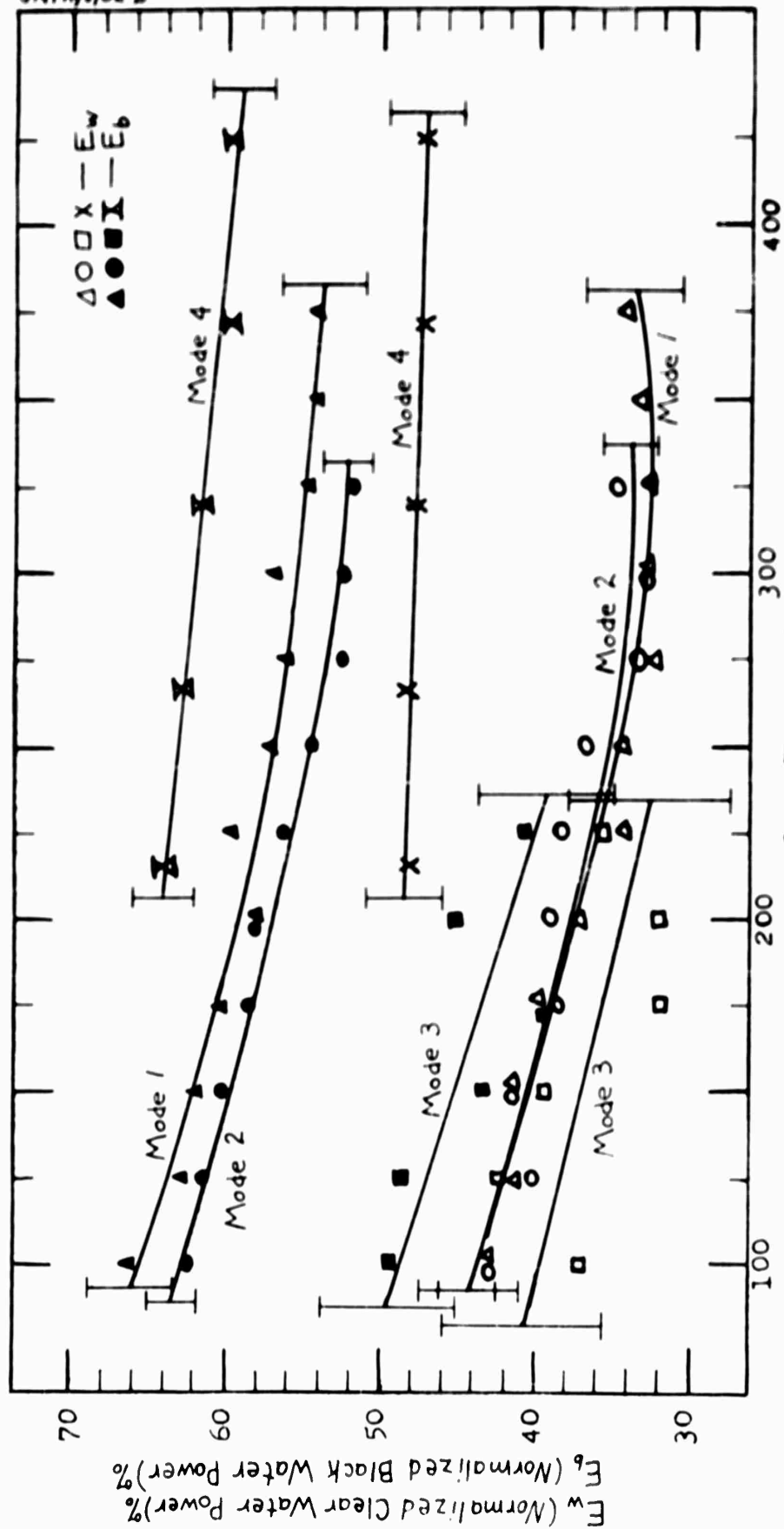
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Fig. 9  
Modified outer tube  
for Mode 3



Gas Flow - Scfh

Fig. 10

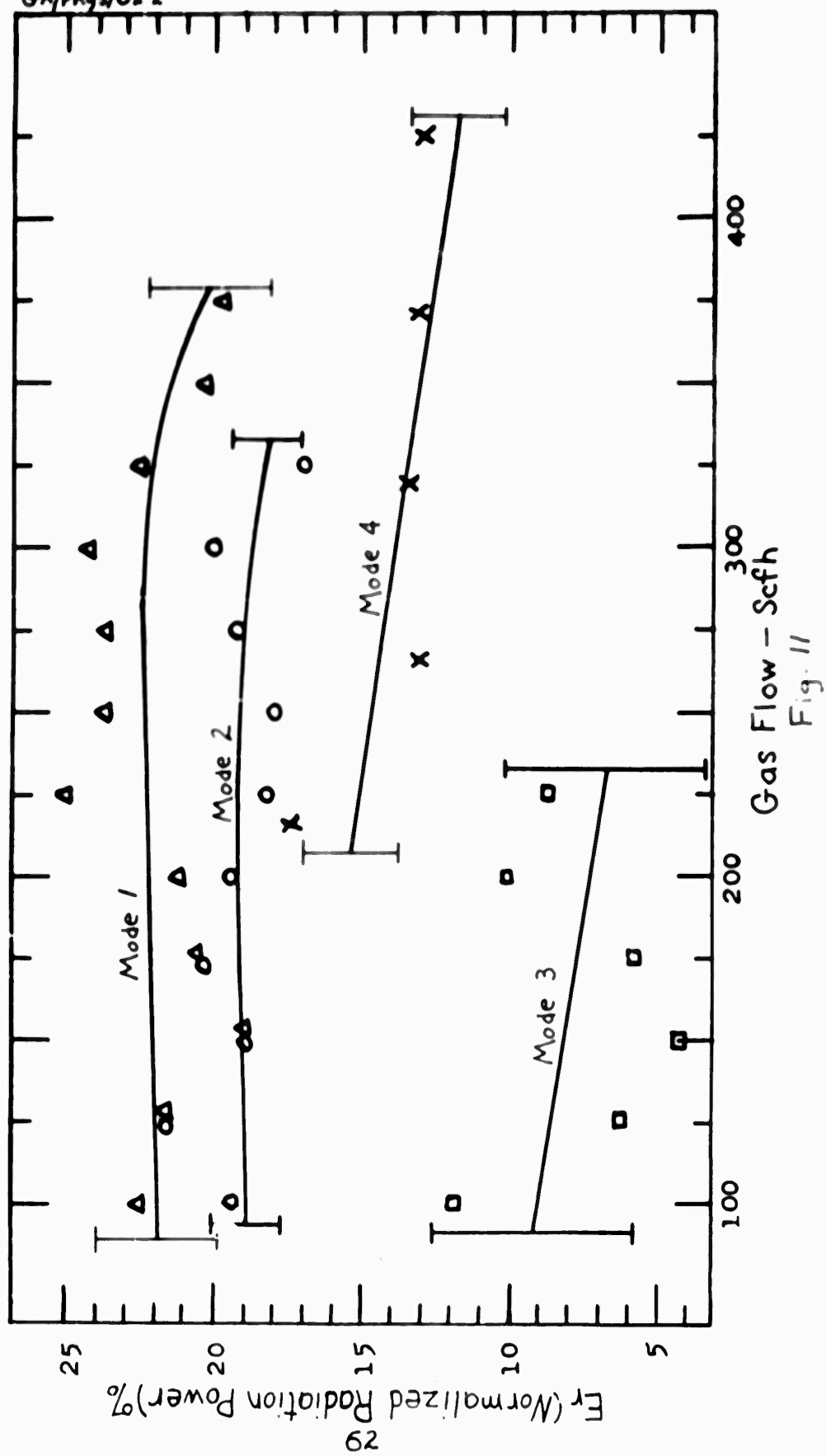
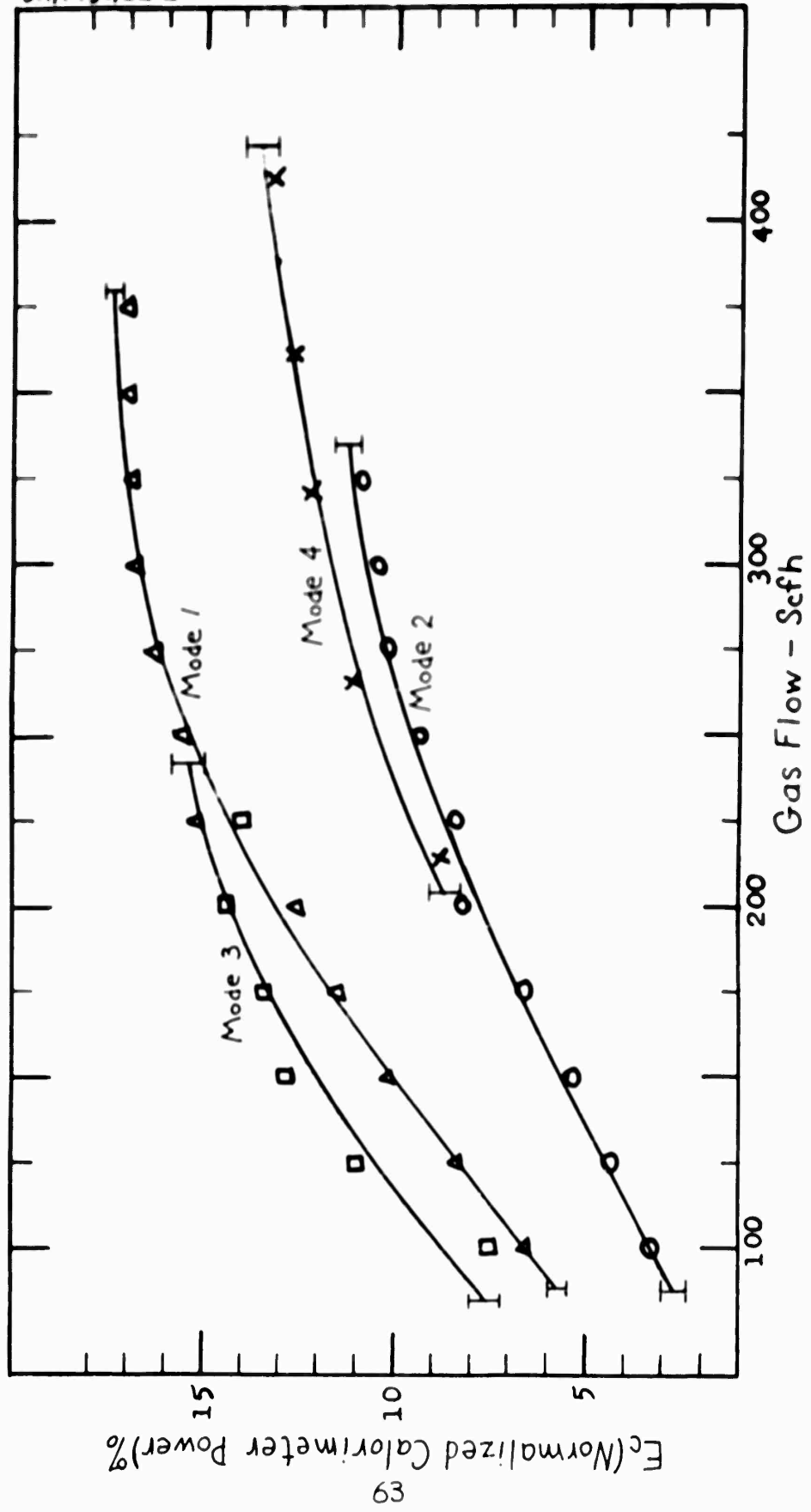
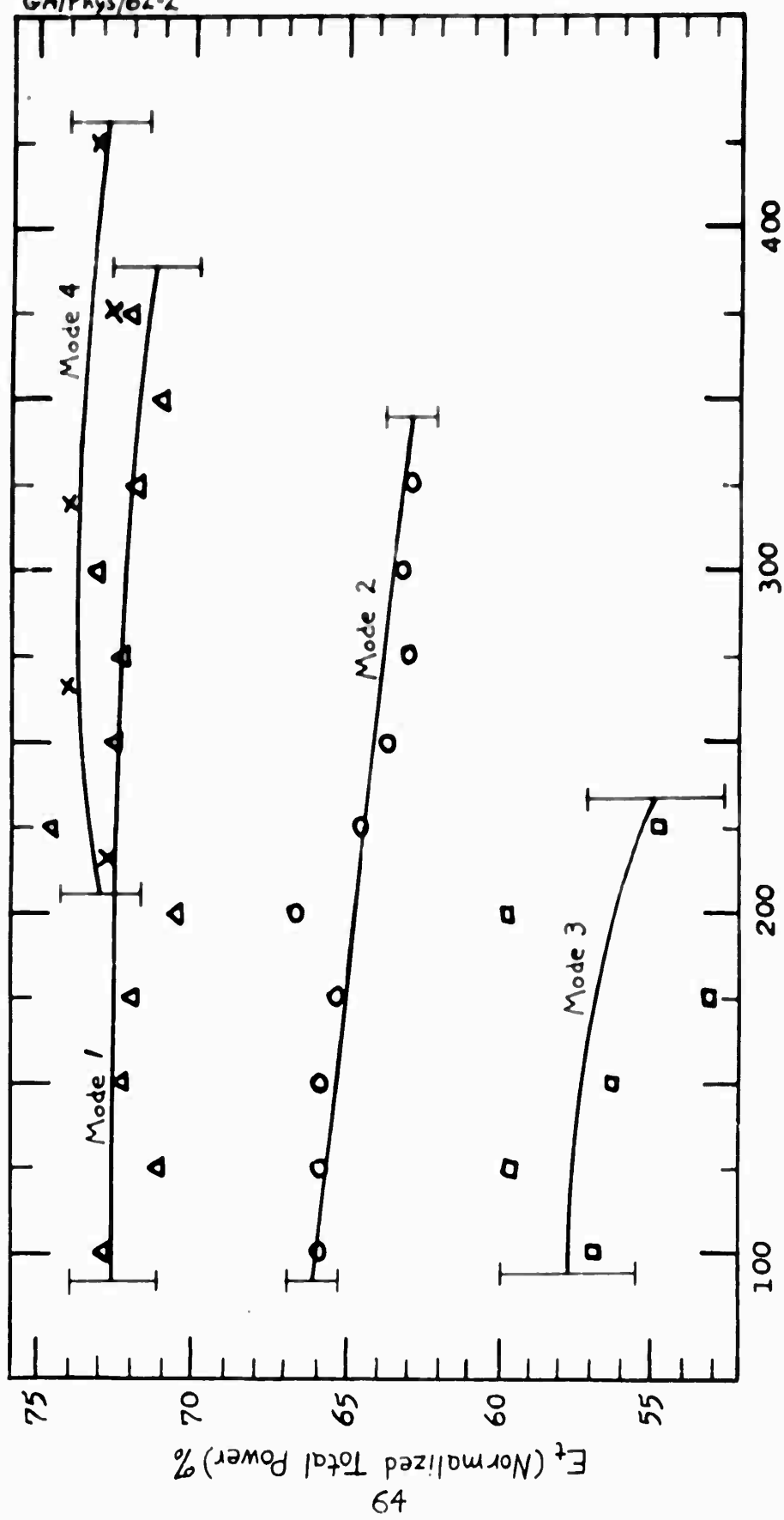


Fig. 11



Gas Flow - Scfh

Fig. 12



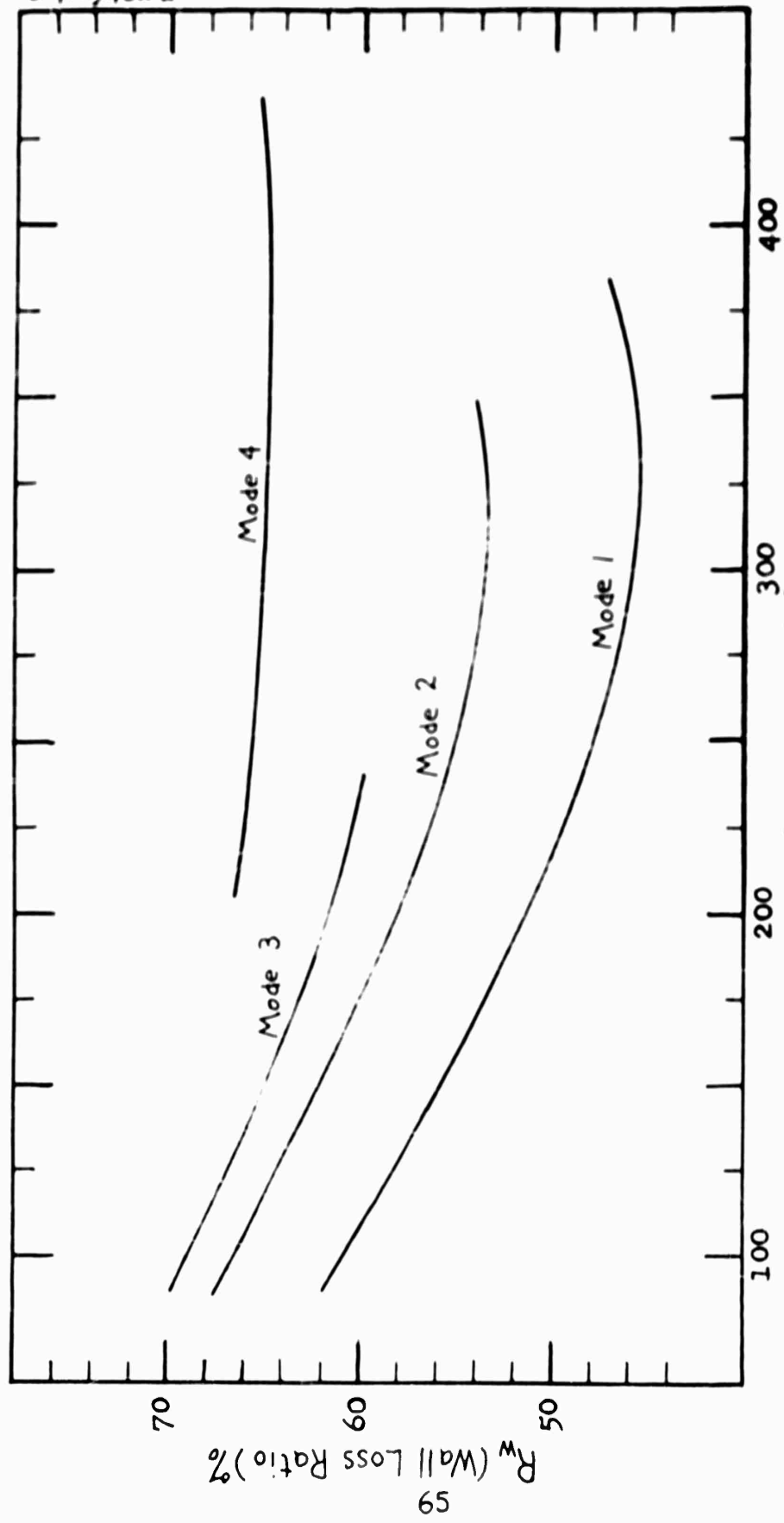
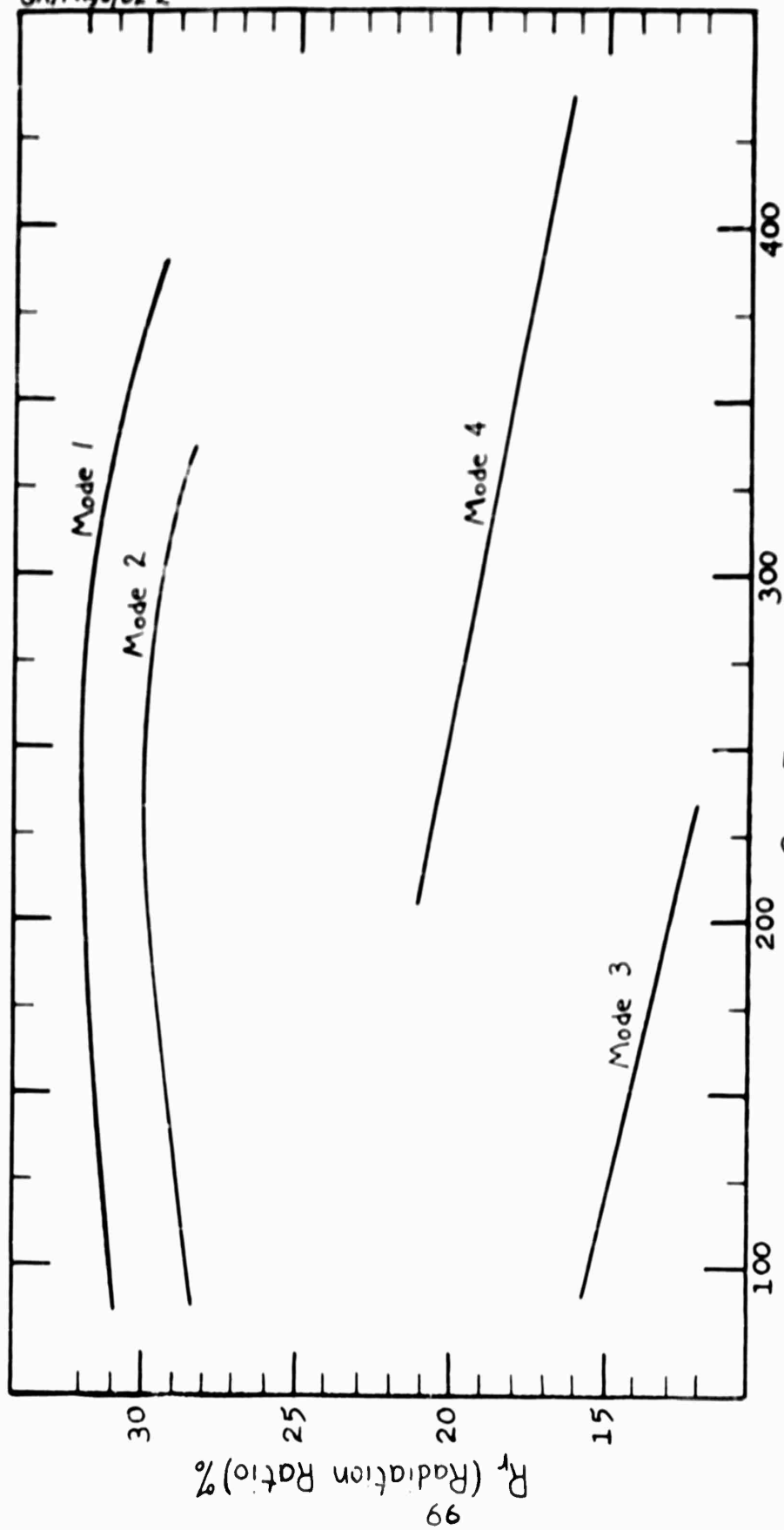


Fig. 14

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Gas Flow - Scfh

Fig 15

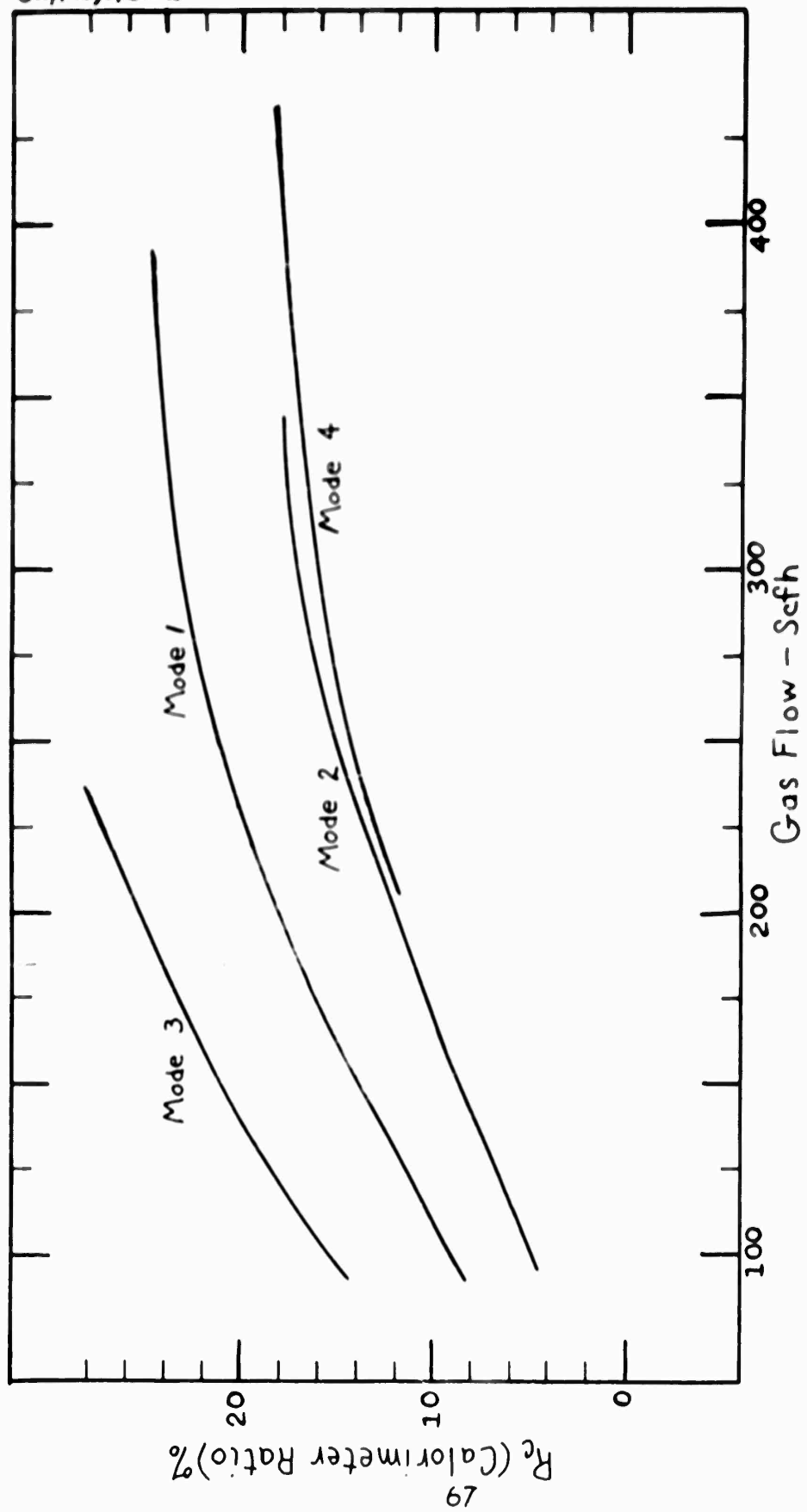


Fig. 16



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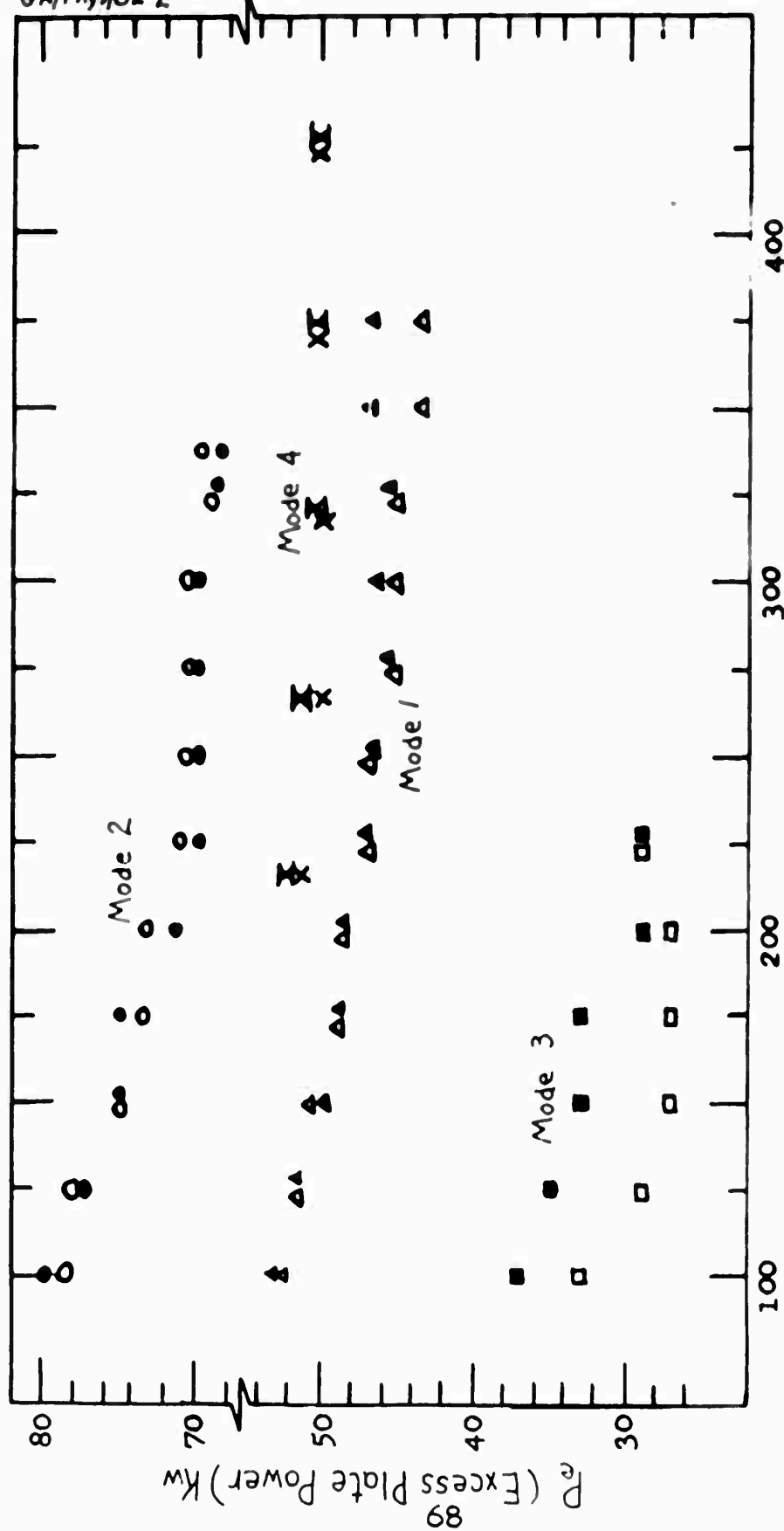


Fig. 17

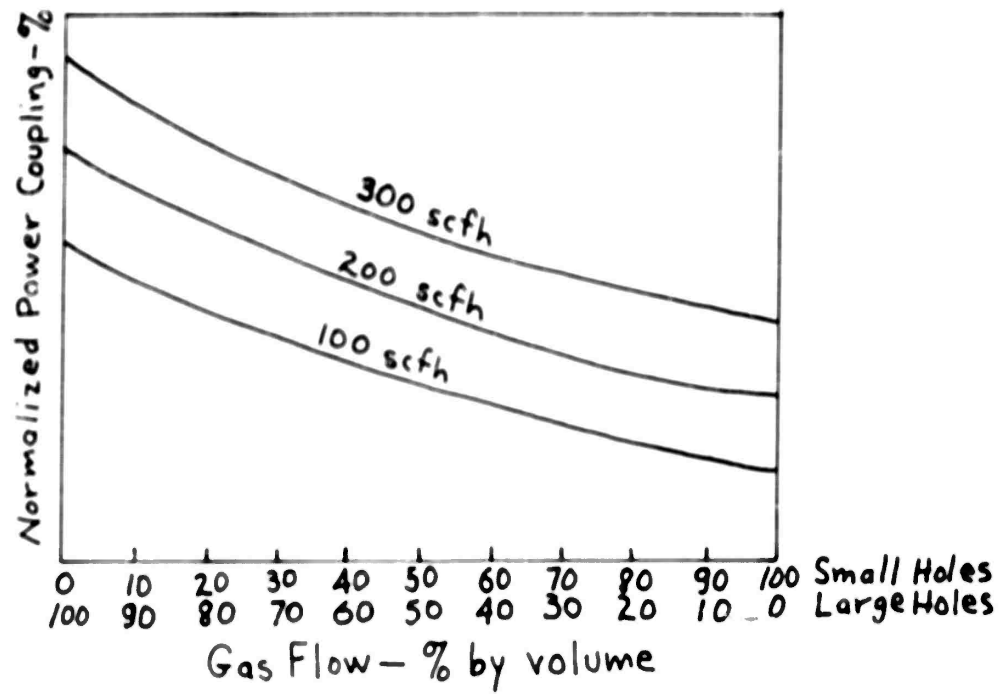
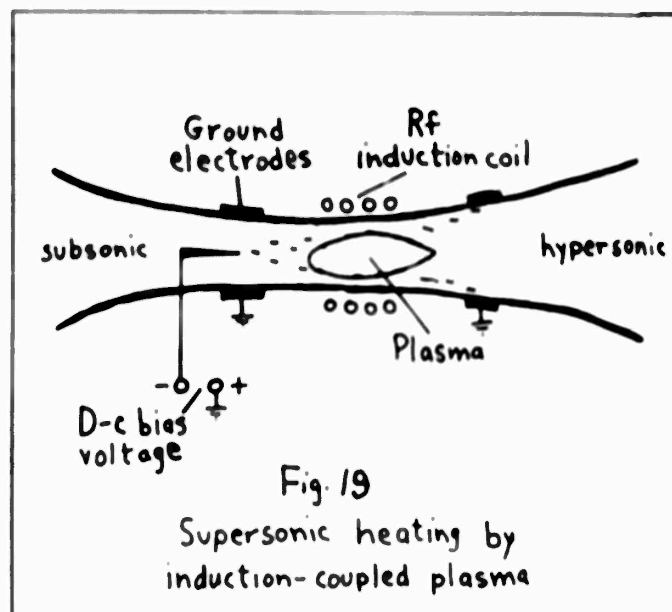


Fig. 18

Power coupling as a function  
of changing vortex strength,  
with excess plate power and  
total gas flow constant



Vita

Howard A. Cannon was born at

[PII Redacted]

He graduated from Northeast High School in Kansas City, Missouri in 1947. In 1948, he enlisted in the United States Air Force, and was appointed to the United States Military Academy from the Regular Air Force in June 1950. On 1 June 1956, he was commissioned a Second Lieutenant in the Regular Air Force, and he graduated from the United States Military Academy on 6 June 1957 with a Bachelor of Science degree in Military Science. Prior to admission to the Air Force Institute of Technology, he served as a visible operations officer in SAC, Korea.

SECRET

Date of birth: 12, '50

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